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Please cite: 1.Grigoropoulos, Georgios; Leonhardt, A.; Kathes, H.; Junghans, M.; Baier, M.; & Busch, F. (2022). Traffic flow at signalized intersections with large volumes of bicycle traffic. Transportation Research Part A: Policy and Practice. <https://doi.org/10.1016/j.tra.2021.11.021>

1 **Traffic flow at signalized intersections with large volumes of bicycle traffic**

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28 **Abstract**

29 The popularity of utilitarian bicycling is increasing in many urban areas. As a result, growing volumes
30 of bicycle traffic on road networks have significant impacts on traffic flow and the capacity of
31 vehicular traffic, particularly at intersections. The goal of this paper is to quantify the impact of large
32 volumes of bicycle traffic on the capacity of signalized intersections concerning vehicular streams
33 crossing the intersection, turning right, and turning left. Empirical studies are conducted to gain
34 insight into the speed, acceleration, queue density, queue discharge, and conflict zone occupancy
35 time of bicycle traffic. Data were collected at sites with varying infrastructure designs and bicycle
36 traffic volumes. The results of the empirical studies are used to assess the effects of bicycle
37 infrastructure on traffic efficiency and build, calibrate, and validate microscopic traffic simulation
38 models. The bicycle traffic volume is incrementally increased in the simulation models to supplement
39 the data from the empirical studies. Based on the empirical findings and simulation results, the
40 average queue discharge time per bicyclist based on the facility width is derived and two factors for
41 the reduction in the capacity of vehicular traffic turning left and turning right based on the actual
42 green time ratio and the volume of crossing bicycle traffic are proposed. If a bike box is present on an
43 intersection approach, findings show that crossing bicycle traffic has a negligible effect on the
44 capacity of crossing vehicular traffic, which bicyclists turning left impede vehicular traffic.

45 **Keywords:** Bicycle traffic, Intersection efficiency, vehicular capacity, Highway Capacity Manual

46

47 **1. Introduction**

48 The bicycle as a mode of transport offers numerous personal and societal advantages including low
49 environmental impacts, negligible noise emissions, a reduction in traffic congestion, minor parking
50 requirements, affordability, and positive health effects. As the potential of bicycling in urban areas is
51 realized, the number of people bicycling and consequently the modal split of the bicycle and the
52 volume of bicycle traffic are increasing. In Germany, the modal split of bicycling increased from 9 %
53 in 2002 to 15 % in 2017 (Nobis and Kuhnimhof, 2019). As expected, the bicycle volume in urban
54 areas has increased accordingly. For example, a continuous counting station installed in Munich,
55 Germany detected just over 1 million bicyclists in 2012. Five years later in 2017, more than 1.3
56 million bicyclists were detected, an annualized increase of approximately 5.4 % per year
57 (Landeshauptstadt München, 2019). Growth of this magnitude has significant consequences on the
58 traffic flow of urban road networks with particularly prominent effects at intersections.

59 As a result of the bicycle traffic growth, new types of bicycle infrastructure are introduced to
60 accommodate the increasing share of bicycle traffic in urban areas. These may include bike boxes

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61 (also called advanced stop lines), bicycle lanes or bicycle paths, or bicycle lanes with advanced stop
62 lines and a stop area for bicyclists downstream of an intersection approach for facilitating an indirect
63 left turn also referred to as a two-stage turn (National Association of City Transportation Officials
64 (NACTO), 2014). Dedicated traffic signal control measures, such as bicycle traffic signal coordination
65 and bicycle traffic prioritization are also introduced in order to improve bicycle traffic efficiency,
66 safety, and the attractiveness of cycling (Baumann, 2016; Grigoropoulos et al., 2019, 2018; Hoegh,
67 2007; Karl and Felix, 2013; Kath et al., 2019; Peter Koonce, 2015; Preethi et al., 2016). However
68 existing tools and methods, such as the ones included in the German Highway Capacity Manual
69 (HBS) (Forschungsgesellschaft für Straßen- und Verkehrswesen (FGSV), 2015) or the American
70 Highway Capacity Manual (HCM) (National Research Council, 2016) that are extensively used by
71 experts to assess the traffic quality and quantify the effects of different design scenarios, are limited
72 in considering the effects of increasing bicycle volumes and new types of bicycle infrastructure on
73 traffic quality.

74 In this paper, the methods for including bicycle traffic in the computation of vehicular capacity at
75 intersections in the HBS are extended to accurately reflect situations with large volumes of bicycle
76 traffic. Thanks to parallels between the methods used in the HBS and other guidelines such as the
77 HCM, these extensions can be useful to practitioners and researchers in many countries. Research
78 was carried out within a German research project and some of the results are presented in German
79 in the final project report (Busch et al., 2019). This paper summarizes and expands this unpublished
80 research, results, and conclusions sections by reviewing additional literature, analyzing the present
81 HCM methodologies for assessing the effects of bicycle volumes on traffic efficiency and capacity, as
82 well as in integrating the proposed adjustments and extensions to the HCM. All references to road
83 user movements in this paper refer to right-hand-traffic (RHT).

84 **2. Related research**

85 The literature review is presented in two parts: First, the behavior of bicyclists is investigated to link
86 this with the effects on traffic capacity. Second, findings of research investigating the effects of
87 bicycle traffic flow on intersection efficiency and capacity are highlighted.

88 *2.1. Behavior of bicyclists at intersections*

89 The tactical behavior includes short term maneuvers chosen consciously by a bicyclist to address
90 specific traffic situations, such as the pathway used when crossing an intersection as well as
91 positioning at a stop (Michon, 1985). According to previous studies, bicyclists exhibit different
92 behaviors based on their maneuver and the traffic state at the intersection approaches (Angenendt et
93 al., 2005; COWI, 2013; Twaddle and Busch, 2019). Bicyclists are found to use the roadway instead

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94 of an available cycling facility if the cycling facility is blocked by an obstacle, the bicyclist is preparing
95 for an anticipated left or right turn maneuver, the bicyclist is not satisfied with the bicycle
96 infrastructure quality or for overtaking (Falkenberg et al., 2003; Kuller et al., 1986). Narrow bicycle
97 lanes (<1m wide) and on-road bicycle lanes are found to have a lower rate of acceptance than other
98 types of bicycle infrastructure (Alrutz et al., 2009).

99 The majority of crossing bicyclists at an intersection use the intended bicycle infrastructure while
100 bicyclists carrying out a turn maneuver are more likely to use the sidewalk (Angenendt et al., 2005;
101 COWI, 2013). Angenendt et al., (2005) investigated the behavior of bicyclists at different types of
102 infrastructure. According to the definition provided by NACTO (National Association of City
103 Transportation Officials (NACTO), 2014), bike boxes (also called advanced stop lines (Allen et al.,
104 2005)) are designated areas at the head of a traffic lane at a signalized intersection that provide
105 bicyclists with a safe and visible way to get ahead of queuing traffic during the red signal phase. If a
106 bike box is available, bicyclists riding straight mainly position themselves less than 2 m from the right
107 side of the bike box (85.3 %) (Angenendt et al., 2005). Another study also found that 78% of
108 bicyclists riding straight use the bike box position themselves in front of motor vehicle traffic in
109 comparison to 54% of bicyclists at approaches without a bike box (Allen et al., 2005). For bicyclists
110 turning left at an intersection, findings indicate that a direct left-turning maneuver is more likely if
111 bicycle infrastructure supporting this type of maneuver is available, such as a bike box or an
112 intermediate bicycle lane for left-turning bicyclists (Angenendt et al., 2005). Thus, left-turning bicycle
113 traffic over a bike box can potentially affect the capacity of motor vehicles as bicyclists position
114 themselves in front of the motor vehicle traffic.

115 Operational behavior, on the other hand, encompasses subconscious actions to control the bicycle
116 within the environment, including speed control, acceleration, deceleration, gap acceptance, and
117 spacing (Michon, 1985). Several studies focus on the relationship between the bicyclist desired
118 speed and the type of cycling facility (Alrutz et al., 2009; Opiela et al., 1980; Schleinitz et al., 2016).
119 The results of these studies are included in the meta-analysis presented by Twaddle (Twaddle,
120 2017), in which a comparison of observed bicyclist speeds as a function of the bicycle infrastructure
121 is presented. The results of the meta-analysis suggest that bicyclist travel at a higher speed on on-
122 road bicycling facilities. Bicycle speeds on separated bicycling facilities and mixed lanes are similar
123 (~5 m/s), with the lowest speeds observed on sidewalks.

124 Bicyclists crossing a prioritized vehicular traffic stream are found to accept time gaps of 3 – 4
125 seconds on average (Kwigizile et al., 2017; Opiela et al., 1980). Motor vehicle drivers crossing a
126 prioritized bicycle traffic stream are found to accept average time gaps of 6 – 7s between crossing
127 bicyclists (Petzoldt et al., 2017).

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129 2.2. *Bicycle traffic efficiency and capacity effects*

130 Several methodologies have been developed to assess the efficiency of bicycle traffic and to
131 consider the effects of bicycle traffic on vehicular traffic at signalized intersections. These
132 methodologies are developed for guidelines assessing traffic flow at signalized intersections, as a
133 part of models to calculate the capacity effects of bicycle traffic on vehicular traffic flow and to
134 calculate the effect of cross-section width on bicycle traffic flow.

135 The HCM evaluates traffic performance at signalized intersections with independent methodologies
136 for motorized and non-motorized modes. The effect of bicycle traffic flow on vehicular traffic flow is
137 considered using adjustment factors. These factors account for the effect of both pedestrian and
138 bicycle traffic flow on the saturation flow of right and left turning vehicular traffic streams and are a
139 function of the expected duration of the occupancy of the conflict zone. The expected duration of the
140 occupancy of the conflict zone is a function of the actual green time ratio and bicycle traffic volume.
141 Chen et al. (2014) developed a platoon width model and a polynomial regression model, which are
142 used to generate an adjustment factor for the saturation flow calculation in the HCM for left-turning
143 motor vehicles.

144 A Level of Service score is described in the HCM for non-motorized traffic based on multiple
145 parameters describing the traffic performance and intersection characteristics. This method for non-
146 motorized modes is limited to intersection approaches with less than a 2 % gradient. Additionally,
147 bicycle traffic delay is calculated and assessed independently of the Level of Service score. For this
148 calculation, bicycles are considered to ride on the road on a dedicated facility (e.g. bicycle lane).
149 Bicycles that travel on the road in mixed traffic are assumed to experience the same delay as
150 vehicular traffic. The bicycle traffic capacity is a function of the effective green time share and the
151 bicycle saturation flow (2000 bicycles/h). It is assumed that bicyclists do not experience any
152 incremental delay or initial queue delay, bicyclists are intolerant to delays over 30 s/bicycle and
153 comply with the traffic signal indication if their expected delay is less than 10 s/bicycle.

154 Bicycle traffic is considered in the HBS as a source of impendence for the movements of partially
155 conflicting streams of motor vehicles, for example by assessing the occupancy of the bicycle-vehicle-
156 conflict zone for vehicles turning right. In this case, the capacity is reduced based on the number of
157 bicyclists and pedestrians occupying the conflict area in each cycle. At the same time, bicyclists are
158 considered part of the opposing traffic flow (PCU = 1) for permitted left-turn movements. The Level of
159 Service for non-motorized traffic is based on the maximum waiting time for the complete crossing of
160 an intersection approach.

161 In both the HCM and the HBS, the capacity is a critical parameter for the calculation of the Level of
162 Service or other traffic quality parameters. When it comes to the capacity of bicycle traffic

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163 infrastructure, capacity values found in the literature range significantly (Botma and Papendrecht,
164 1991; Greibe and Buch, 2016; Hein et al., 2013; Jin et al., 2017; Li et al., 2015; Pu et al., 2017) and
165 depend primarily on available width, number of lanes, bicycle type and bicycle desired speed. Bicycle
166 traffic capacity is found to be linearly dependent on the bicycle infrastructure width. The capacity
167 increases by 1.11 bicycles/s for every additional meter path width in the range of 0.50– 1.50 m width
168 (Wierbos et al., 2019). In the case of the HCM, the bicycle infrastructure width is considered in the
169 calculation of the bicycle delay and not in the calculation of the bicycle traffic capacity. In the HBS, no
170 special methodology for estimating the capacity of bicycle traffic at a signalized intersection approach
171 is presented. The number of lanes, bicycle type, and bicycle desired speed is not considered. Finally,
172 no special considerations are made concerning special types of bicycle infrastructure such as bike
173 boxes or approaches with stop areas for indirect left turning.

174 Several researchers have suggested methods for analysing the capacity of signalized intersections
175 with bicycle traffic and modelling bicycle traffic performance. Chen et al. (2009) present a
176 methodology for calculating capacity considering the influence of bicycle blockage, waiting bicyclists
177 in partially conflicting streams, traversing bicyclists and bicyclists waiting inside the intersection. A
178 similar approach in which models are developed to quantify the effects of bicycle traffic on the
179 saturation flow of the turning vehicles by defining different stages of bicycle movements is proposed
180 by Guo et al. (2012). Allen et al. (1998) proposed, calibrated, and validated a model for estimating
181 the share of the green phase in which the conflict area is occupied using bicycle traffic volume as an
182 input. Another study assesses the Level of Service based on traffic volume, the total width of the
183 outside through lane, and the intersection crossing distance for through movements (Landis et al.,
184 2003). Finally, researchers in the Netherlands studied the bicyclist queue discharge process at a
185 signalized intersection approach. The bicyclist jam density is found to positively influence the queue
186 discharge rate and a regression model was fitted to the empirical data. The results were validated
187 through an experimental study with test subjects. A bicycle discharge rate of 1.2 to 1.4 bicycle/s was
188 measured in the experiment (cross-section width = 3m) while a rate of 1.5 bicycle/s was measured
189 at the intersection approach (width = 3m two-way bicycle path) (Wierbos et al., 2020). In general,
190 most models developed to account for the influence of bicycle traffic at signalized intersections focus
191 on mixed traffic conditions and do not account for the influence of bicycle infrastructure. Models that
192 estimate the capacity effects of bicycle traffic on vehicular traffic typically utilize the occupancy
193 duration of the conflict area between motor vehicles as the critical traffic parameter. Such models are
194 mostly not easily integrated into the existing methods in the HCM and HBS due to their inherent
195 complexity. Thus, our research aims to propose methods that can be easily integrated into existing
196 methods for assessing the effect of different bicycle traffic streams and bicycle infrastructure on the
197 intersection capacity.

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198 3. Method

199 The aim of this research is to analyse the traffic flow at signalised intersections with a high bicycle
200 traffic volume and, develop new methods that can integrate into existing methods for assessing the
201 effect of different bicycle traffic streams and bicycle infrastructure on the intersection capacity.

202 Results from past research contribute the development of the methodology followed to develop new
203 methods for assessing the effect of bicycle traffic and bicycle infrastructure on intersection capacity.

204 Empirical studies at signalized intersections are necessary to gain insights on bicyclist behaviour
205 using different types of bicycle infrastructure and their interaction with motor vehicle traffic. The
206 estimation of the effect of large volumes of bicycle traffic on the flow of vehicular traffic at signalized
207 intersections is based on the combination of results coming from empirical studies and simulation
208 studies. In a first step, study intersections with different types of bicycle infrastructure are selected.
209 Empirical studies are carried out to measure the acceleration, speed, queue density, and discharge
210 time as well as the occupancy duration of conflict zones between bicycle and vehicular traffic. These
211 parameters provide the basis for subsequent simulation studies. Simulation studies are required as a
212 complete, representative empirical survey of all relevant cases and variations of bicycle infrastructure
213 and signalization (traffic infrastructure parameters) combined with different traffic compositions are
214 not feasible only through empirical observations. Simulation studies also allow the analysis of
215 scenarios or intersection characteristics that are not included in the study intersections as well as the
216 measurement of parameters that are difficult to estimate empirically. Therefore, data collected in the
217 empirical studies are used to calibrate and validate microscopic traffic simulation models. The
218 volume of bicycle traffic is increased incrementally in the simulation to derive the effect of large
219 volumes of bicycle traffic on vehicular traffic flow. The empirical data and the output of the simulation
220 studies are used to propose adjustments to the calculation methods in the HBS. Finally, general
221 recommendations for other capacity manuals are derived.

222

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223 3.1. Empirical studies

224 A survey of possible study sites was conducted across German cities to identify possible study
225 intersections. Intersection approaches with high gradients or other types of environmental factors that
226 could potentially influence the bicyclist driving behavior were not considered. After the initial search,
227 a total of 32 intersections were considered for the video data collection across six different German
228 cities. Eventually, to analyse motor vehicle and bicycle traffic flow at signalized intersections with
229 varying types of cycling infrastructure, data were collected at eight intersections in Germany (two
230 intersections in Berlin, two intersections in Freiburg, and four intersections in Munich). The study
231 intersections are presented in Table 1.

- 232 1. B3: Intersection Berlin, Karl-Liebknecht-Strasse / Spandauer Strasse
- 233 2. B4: Intersection Berlin, Oranienburger Strasse / Friedrichstrasse
- 234 3. FR3: Intersection Freiburg, Lehner Strasse / Eschholzstrasse
- 235 4. FR6: Intersection Freiburg, Eschholzstrasse / Basler Strasse / Lörracher Strasse
- 236 5. M1: Intersection Munich, Marsstrasse / Seidlstrasse
- 237 6. M2: Intersection Munich, Arnulfstrasse / Seidlstrasse
- 238 7. M3: Intersection Munich, Kapuzinerplatz
- 239 8. M4: Intersection Munich, Schellingstrasse / Luisenstrasse

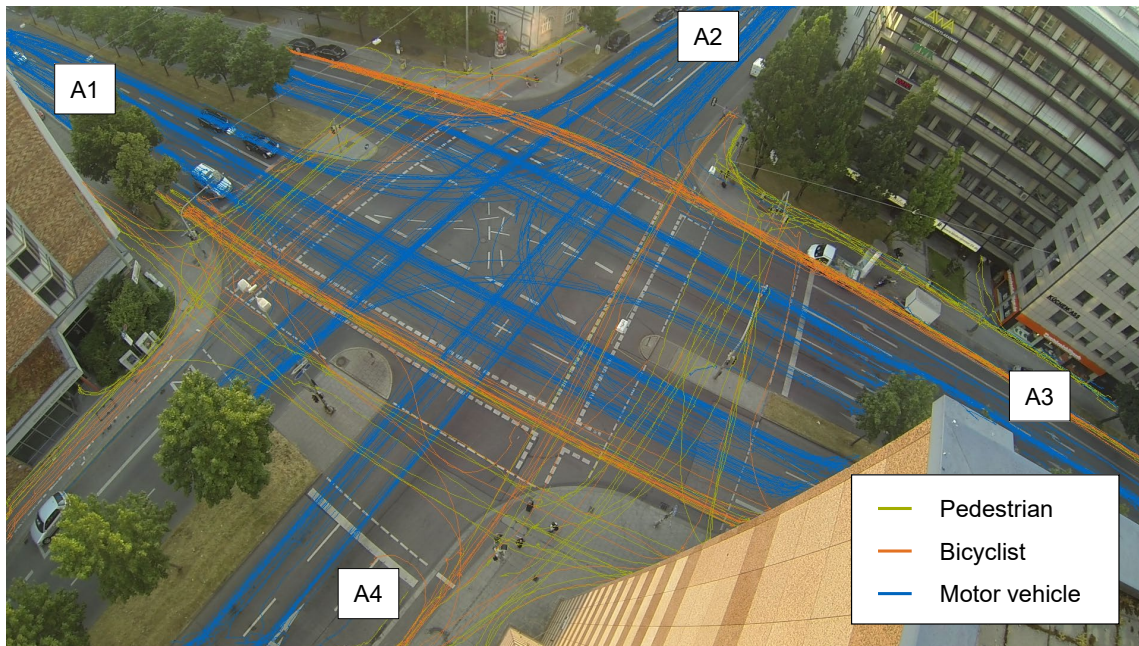
240 The study intersections were selected based on three criteria:

- 241 1. Best possible coverage of infrastructure design options according to the Guidelines for Urban
242 Road Design (German: Richtlinien für die Anlage von Stadtstraßen, RASt)
243 (Forschungsgesellschaft für Straßen und Verkehrswesen (FGSV), 2006) and the
244 Recommendations for Cycling Facilities (German: Empfehlungen für Radverkehrsanlagen,
245 ERA) (Forschungsgesellschaft für Straßen und Verkehrswesen (FGSV), 2010).
- 246 2. High volumes of bicycle traffic.
- 247 3. Practical possibilities for collecting video data, including a high building in near proximity of
248 the intersection or space to park the Urban Traffic Research Car (UTRaCar) (Deutsches
249 Zentrum für Luft und Raumfahrt, 2020).

250 For a detailed analysis of the operational behavior of bicyclists, trajectories are automatically
251 extracted from the video data and are further processed to extract parameters such as the
252 acceleration and average speed. The video cameras were installed as high as possible and with the
253 best possible viewing angle of the intersection approaches. Two different systems were used for data

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254 collection: a mobile system consisting of two cameras mounted on a 12 m high mast on the
 255 UTRaCar test vehicle. The system was used for data collection in the Berlin study intersections. The
 256 second system consists of a camera installed on a mast or on/in a high building and was used to
 257 collect video data in Munich and Freiburg. Figure 1 shows the camera view from the rooftop of the
 258 building at the Marsstrasse / Seidlstrasse intersection in Munich. Video data were collected during
 259 one day at each intersection. Periods of 1h to 2h duration for each intersection with high traffic
 260 volumes were selected for further analysis. The vehicle trajectories were extracted using automated
 261 image processing methods and are classified according to the vehicle type, such that trajectories of
 262 bicyclists motor vehicles, and pedestrians are available (in orange, blue and yellow in Figure 1).
 263 Trajectory data were manually verified to ensure the accuracy of the automated tracking and
 264 classifying procedures. As no significant interactions were observed among bicyclists and
 265 pedestrians, the pedestrian trajectories were excluded from further analysis.

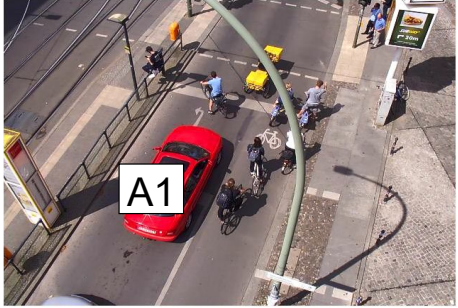



266
 267 Figure 1 Camera view at the intersection Marsstrasse / Seidlstrasse in Munich with extracted
 268 trajectory data.

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270 Table 1 Study intersections.

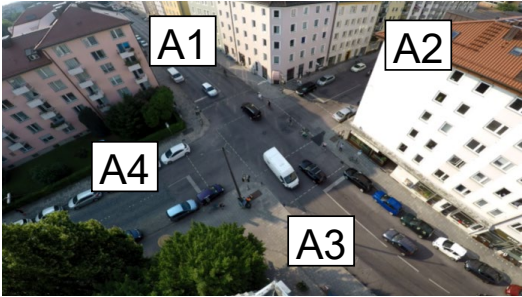
ID	Approach	Bicycle infrastructure type	Bicycle infrastructure width [m]	Bike box size [m ²]	Camera View
B3	A1	Bicycle lane	1.8	-	
B4	A1	Bike box	4.75	23.8	
FR3	A1	Bike box	7	35	
	A2	Bike box	6.5	39	
FR6	A1 (L1)	Bicycle lane	1.5	-	

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ID	Approach	Bicycle infrastructure type	Bicycle infrastructure width [m]	Bike box size [m ²]	Camera View
A1 (L2)			1.8	-	
M1	A1	Bicycle lane	2.0	-	
	A2	Bicycle path	1.8	-	
	A3	Bicycle lane	2.0	-	
	A4	Bicycle path	1.5	-	
M2	A1	Bicycle lane	2.0	-	
	A2	Special form	-	-	
	A3	Bicycle path	1.6	-	
	A4	Bicycle path	2.2	-	
M3	A1	Bicycle lane	2.5	-	
	A2	Bicycle path	1.5	-	
	A3	Bicycle lane	2.5	-	

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ID	Approach	Bicycle infrastructure type	Bicycle infrastructure width [m]	Bike box size [m ²]	Camera View
M4	A1	Mixed traffic	-	-	
	A2	Mixed traffic	-	-	
	A3	Mixed traffic	-	-	
	A4	Mixed traffic	-	-	

271

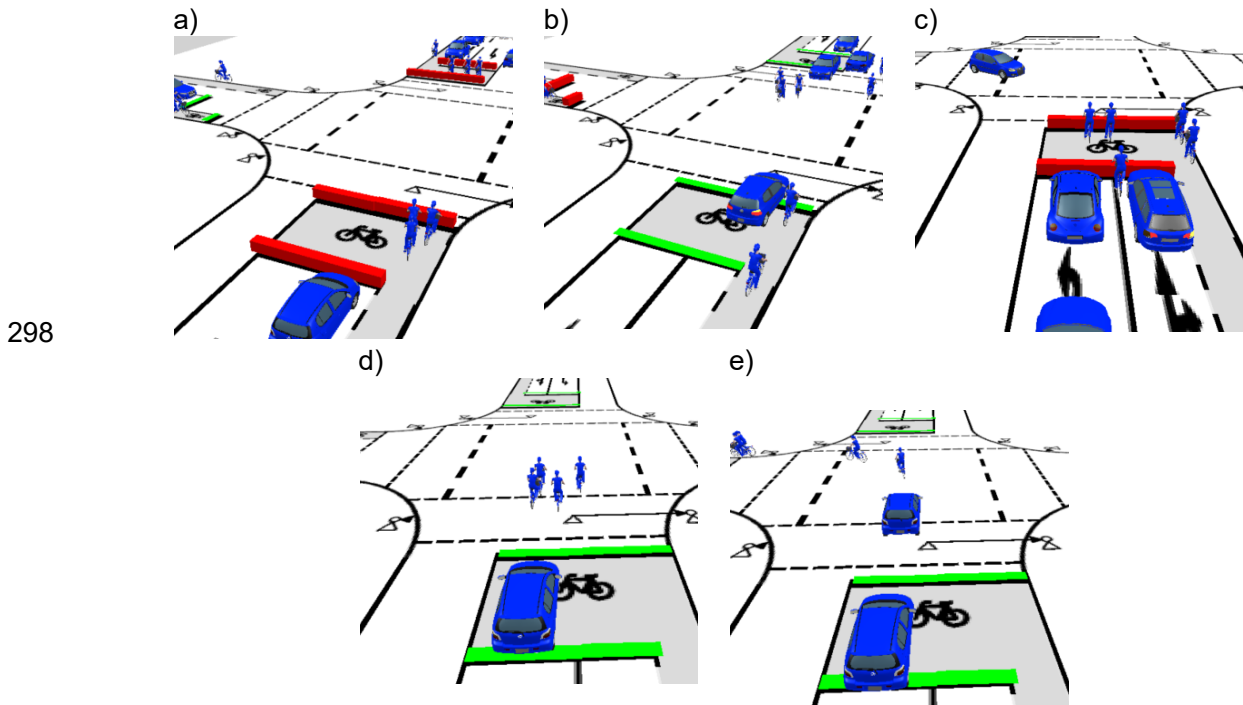
272 *3.2. Simulation studies*

273 Simulation is used to extrapolate empirical findings to other traffic scenarios and bicycle
 274 infrastructure, and to derive data that is typically not observable (capacities). The results from the
 275 empirical studies and the literature findings serve as the basis for the creation of simulation models.
 276 The results of Angenendt et al.(2005) on the lateral positioning of bicyclists with respect to different
 277 available types of bicycle infrastructure (bike boxes, bicycle lanes and bicycle paths) and the results
 278 on the respective bicyclist desired speeds are used for the design of the simulation models in
 279 combination with the results from the empirical studies. The literature results on the bicyclist speed
 280 distribution, the desired speed and the acceleration behavior confirm the findings from the empirical
 281 studies and are used to model the bicyclist operational behavior (Figliozzi et al., 2013; Parkin and
 282 Rotheram, 2010; Taylor, 1993; Twaddle and Grigoropoulos, 2016). Finally, the cumulative speed
 283 distribution function of bicyclists generated using the trajectory dataset from the empirical studies
 284 Figure 7 (right) confirms findings from past research (Falkenberg et al., 2003).

285 PTV Vissim was used to carry out the simulation studies. PTV Vissim is a software for multi modal
 286 microscopic traffic flow simulation. It includes dedicated behavior models for bicyclists and their
 287 interaction with motorized vehicles. Particularly important features are the realistic lateral movement
 288 and positioning of the bicyclists according to the observations in the video recordings. Figure 2
 289 shows impressions from a simulation model with a bike box. As observed in the empirical studies,
 290 simulated bicyclists riding straight across the intersection remain within the width of the bicycle lane
 291 and do not make use of the entire bike box (Figure 2a). These bicyclists mainly hinder the movement
 292 of motor vehicles turning right (Figure 2b). Motor vehicles crossing the intersection are delayed if

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293 several bicyclists wait or ride two or more abreast. Bicyclists turning left using a direct maneuver
 294 (Figure 1) usually move into the left lane upstream of the intersection, pass waiting motor vehicles,
 295 and queue in front of the vehicles in the bike box (Figure 2c). At the start of the green phase, these
 296 bicyclists ride as a group in front of vehicles (Figure 2d) and turn into the bicycle lane or pathway on
 297 the right side of the road, if available (Figure 2e).



299 Figure 2 Impressions of road user behavior on the simulated bike box (PTV VISSIM).

300 The simulation models are based on example study intersections with typical infrastructure design
 301 and dimensions are created according to the design guidelines in the German Guidelines for Urban
 302 Road Design (German: RAS - Richtlinie für die Anlage von Stadtstraßen) (Forschungsgesellschaft
 303 für Straßen und Verkehrswesen (FGSV), 2006) and Recommendations for Cycling Facilities
 304 (German: ERA - Empfehlungen für Radverkehrsanlagen) (Forschungsgesellschaft für Straßen und
 305 Verkehrswesen (FGSV), 2010) (see Figure 11).

306 4. Results

307 4.1. Empirical studies

308 Video data were collected at each of the intersections on a weekday during the summer months
 309 when the volume of bicycle traffic is particularly high. Depending on the conditions at the intersection,
 310 the UTRaCar, an adjacent building, or a mast are used to mount the video camera(s).

Please cite: 1.Grigoropoulos, Georgios; Leonhardt, A.; Kathis, H.; Junghans, M.; Baier, M.; & Busch, F. (2022). Traffic flow at signalized intersections with large volumes of bicycle traffic. Transportation Research Part A: Policy and Practice. <https://doi.org/10.1016/j.tra.2021.11.021>

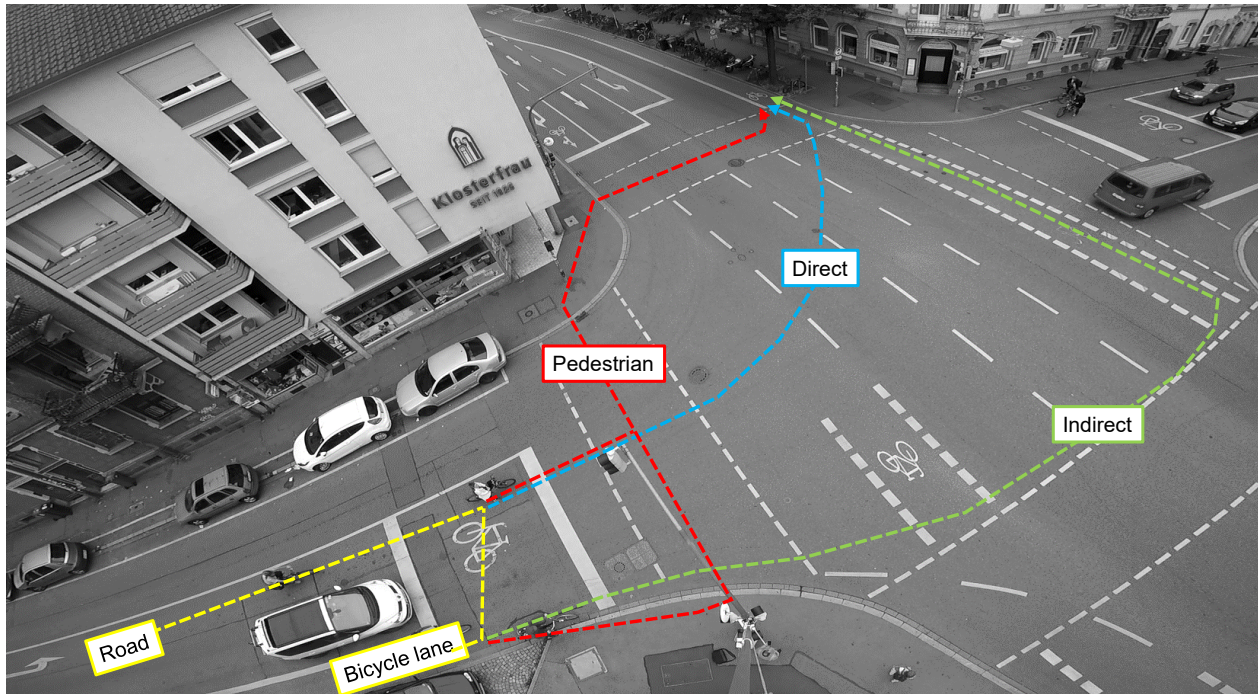
311 In the first step of the analysis, the segments of the video data are viewed manually to gain insights
 312 into the queuing behavior of bicyclists on separated bicycle paths, on-road bicycle lanes, and bike
 313 boxes as well as the behavior of bicyclists turning left. It is possible that bicyclists are adapting their
 314 behavior according to the respective infrastructure, the traffic situation, or the traffic signal state.
 315 Also, it had to be ensured that in the recorded data no irregular or recurring obstruction of bicycle
 316 traffic flow was taking place by other road users.

317 Table 2 presents the total number of road users detected in each intersection for each analysis
 318 period. Figure 3 shows a schematic of the routes used by bicyclists turning left on one approach
 319 using as an example the Lehener Strasse / Eschholzstrasse intersection in Freiburg. The percentage
 320 of bicyclists observed carrying out each type of left turn is shown in Figure 4.

321 It is found that bicyclists approaching the intersection on the road and using the bike box proceed to
 322 carry out a direct left turn. About a fifth of the bicyclists arriving during the red phase uses the
 323 pedestrian crosswalk to cross the street (about 26% of those approaching on the road and about 4%
 324 of those approaching on the bicycle lane) in an effort to avoid a stop and reduce their delay at the
 325 intersection approach. Eventually at this intersection, due to the bike boxes, only a very small
 326 proportion of bicyclists turn left indirectly, as the respective indirect left turn shares significantly
 327 increase in the other examined intersection where no such infrastructure is provided (see Figure 5
 328 and Figure 6). These findings highlight the importance of bike boxes in enabling the direct left turn
 329 maneuver for bicycle traffic.

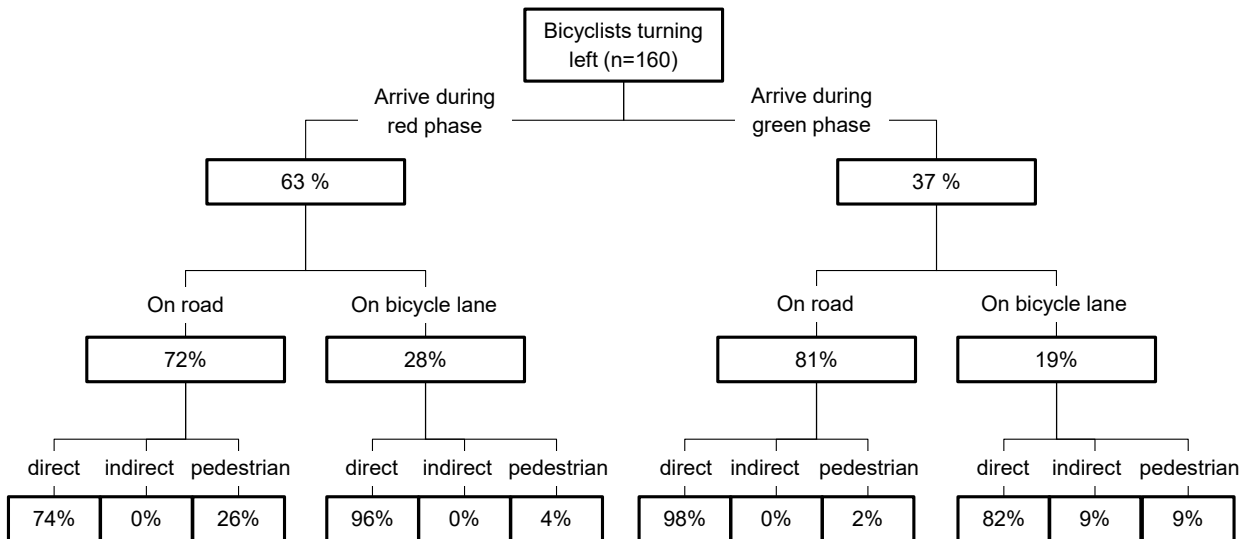
330 Table 2 Total number of detected road users per intersection for the analysis period.

ID	Analysis period (hr)	Total bicycles	Total motor vehicles
B3	3	795	945
B4	2	926	369
FR3	2	1964	4342
FR6	2	361	1462
M1	2	1412	7256
M2	2	1440	4768
M3	2	2458	4210
M4	1	579	852



332

333 Figure 3 Types of observed left turn pathways



334

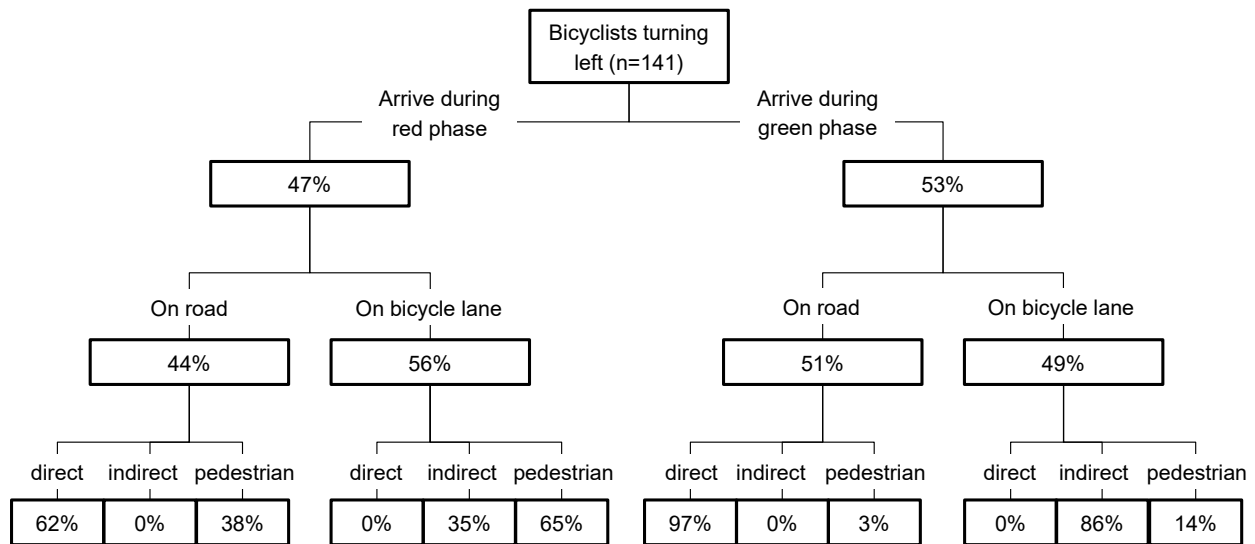
335 Figure 4 Proportion of bicyclists observed using each type of left turn at the Lehener Strasse

336 /Eschholzstrasse intersection in Freiburg.

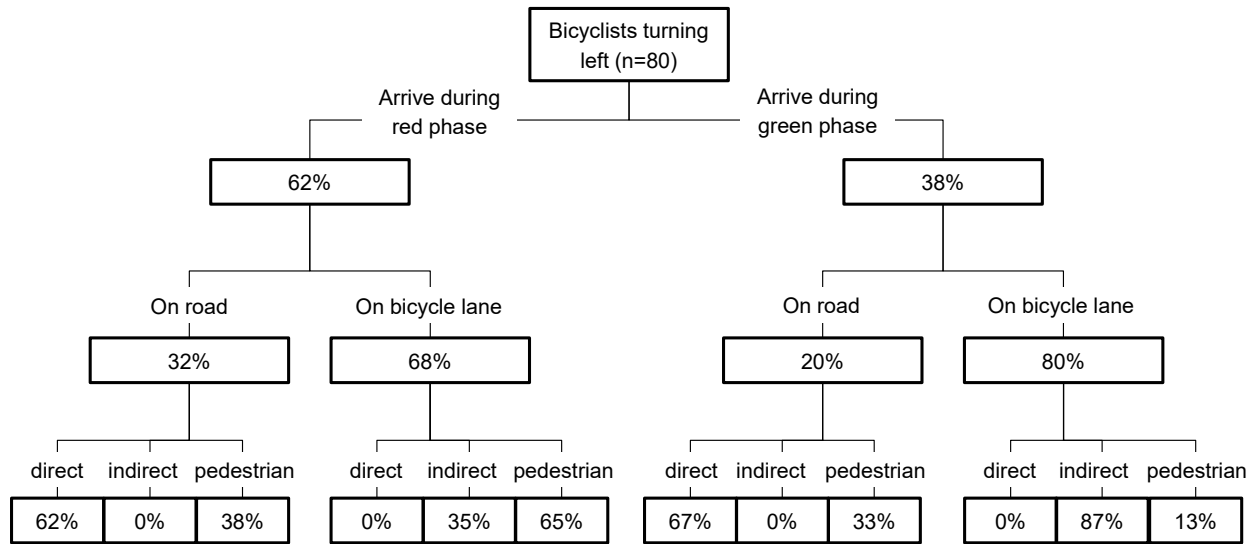
337 At intersection Kapuzinerplatz (M3) (Table 1) the left-turning bicyclists use the bicycle lane and the
 338 road in roughly equal parts. At this intersection, bicyclist lanes are provided only for bicycle traffic
 339 riding straight at the intersection. A downstream bicyclist stop area is provided for left turning
 340 bicyclists. Most bicyclists riding on the road and arriving at the intersection approach during the green
 341 phase performed a direct left turn (97%), while most bicyclists riding on the bicycle lane and arriving

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342 at the intersection approach during the green phase performed an indirect left turn (86%). At the
 343 same time, bicyclists riding on the road and arriving at the intersection during the red phase
 344 performed a direct left turn (62%), while 38% used the pedestrian crossing to turn left, to reduce their
 345 expected delay at the intersection. Finally, 65% of bicyclists riding on the bicycle and arriving at the
 346 intersection during the red phase used the pedestrian crossing while 35% proceeded to an indirect
 347 left turn. These results signify the differences in the left turning behavior between bicyclists using the
 348 respective available infrastructure in the form of bicycle lanes, pedestrian crossings or downstream
 349 bicyclist stop areas and bicyclists that are not, showing that bicyclists making use of the available
 350 bicycle infrastructure also tend to use bicycle or pedestrian infrastructure to perform their intended
 351 maneuver and do not mix with motor vehicles. Also, the same group of bicyclists made use of the
 352 available bicycle infrastructure to turn left when arriving during the green phase, while upon during
 353 the red phase, made use of the pedestrian crossing in an effort to reduce their delay. Empirical
 354 results are presented in Figure 5.



355
 356 Figure 5 Proportion of bicyclists observed using each type of left turn at the Kapuzinerplatz
 357 intersection in Munich.



358
359 Figure 6 Proportion of bicyclists observed using each type of left turn at the Marsstraße/Seidlstraße
360 intersection in Munich.

361 At the intersection M1 Marsstraße/Seidlstraße (Table 1) most bicyclists make use of the bicycle lane
362 or bicycle path to turn left. The majority of bicyclists riding on the road will perform a direct left turn
363 regardless of the traffic signal state (62% when arriving during red phase and 67% when arriving
364 during green phase). However, this does not apply for bicyclists using the bicycle lane as they will
365 turn left either using the pedestrian crossing during the red phase (65%) or use perform an indirect
366 left turn during the green phase (87%), effectively adjusting their behavior to reduce their expected
367 delay at the intersection. Empirical results are presented in Figure 6.

368 Results across the three intersections suggest that most bicyclists will make use of dedicated bicycle
369 infrastructure if such is provided at the intersection approach and directly facilitates their intended
370 maneuver. However, in the absence of dedicated bicyclist infrastructure, it is more probable that
371 bicyclists will make use of motor vehicle or pedestrian infrastructure to execute their intended
372 maneuver and adjust their behavior and infrastructure choice depending on the traffic signal state.
373 These results are also supported by previous research (Twaddle and Busch, 2019).

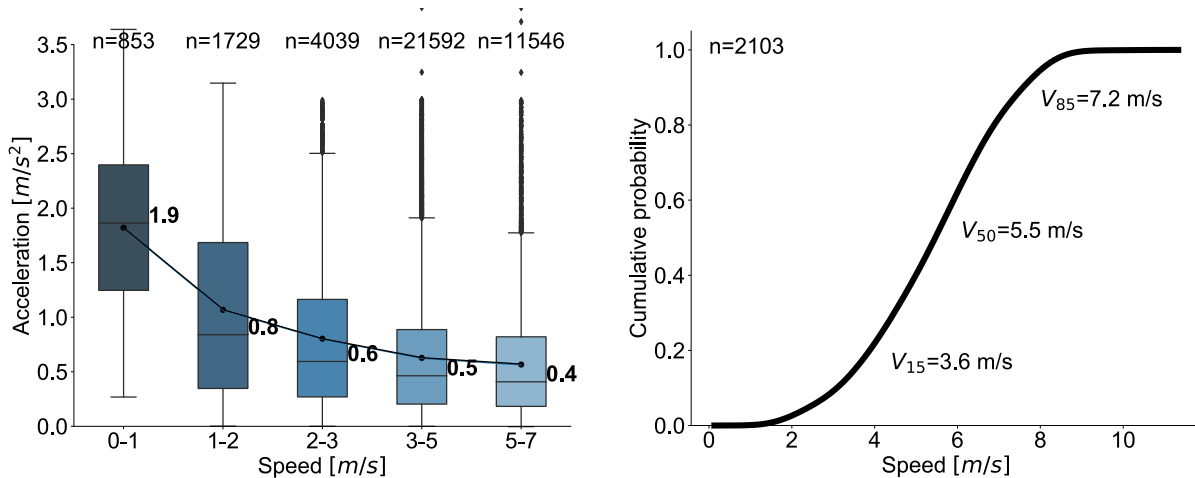
374 In the second step of the analysis, trajectories are automatically extracted from the video data and
375 are further processed to extract parameters such as the acceleration and average speed. The
376 parameters determined from the bicyclist trajectories are explained below and presented with an
377 example evaluation:

- 378 • **Acceleration from stop:** The acceleration from a complete stop at the beginning of the
379 green phase directly affects the queue discharge time and the time in which bicyclists occupy
380 the conflict zone with vehicles turning left and right. It is therefore an essential parameter for

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381 the parameterization of driving behavior in the simulation. Figure 7 (left) shows acceleration
 382 as a function of speed at the Marsstrasse / Seidlstrasse intersection in Munich as an
 383 example. The sample size n refers to the total number of bicyclist acceleration recordings in
 384 all observed bicyclist positions along their respective trajectories.

385 • **Desired speed distribution:** This is an important parameter to create realistic bicycle traffic
 386 in simulation models. Because the desired speed cannot be measured directly, the mean
 387 speed travelled by each observed bicyclist after completion of the acceleration process is
 388 taken as a surrogate measure. The cumulative density function of the desired speed
 389 surrogate measure from all research intersections is shown in Figure 7 (right). The sample
 390 size n refers to the total number of bicyclist acceleration recordings in all observed bicyclist
 391 positions along their respective trajectories.

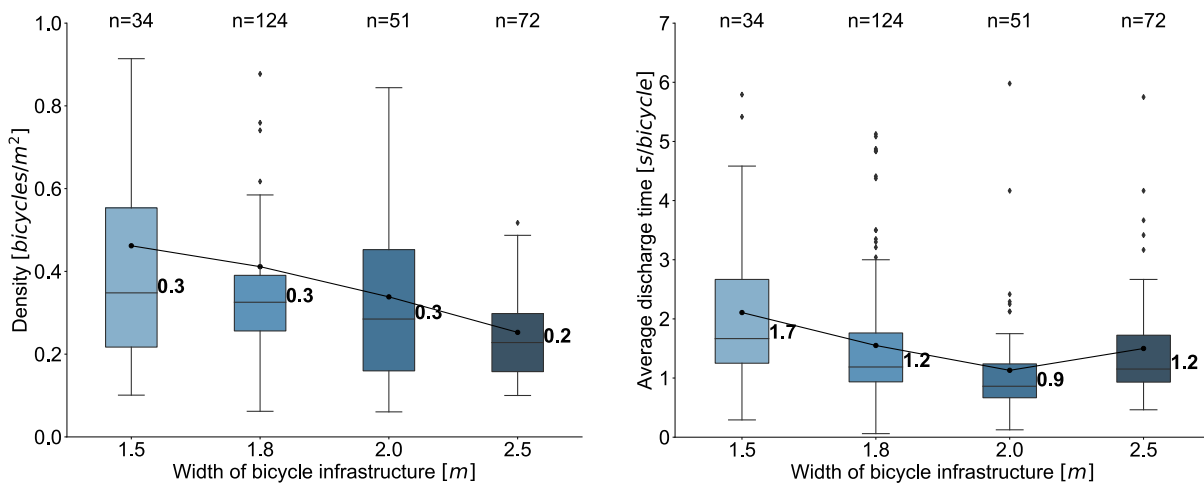


392
 393 Figure 7 Observed acceleration as a function of speed (left) and cumulative density functions for the
 394 desired speed (right).

395 • **Queue density:** This parameter describes the number of bicyclists per square meter in a
 396 queue at a stop line on a cycling facility. It is calculated by dividing of the number queued
 397 bicyclists at the start of green time by the area formed by the respective infrastructure width
 398 and the length of the present queue (measured from the stop line). The queue density can
 399 serve both as a calibration parameter for traffic simulation and the design of road
 400 infrastructure (dimensioning of waiting areas at stop lines). The observed queue density for
 401 bicycle lanes and separated bicycle paths are shown in Figure 8 (left). The sample size n
 402 refers to the number of analysed queues.

403 • **Average discharge time:** This parameter indicates how long it takes on average for each
 404 bicyclist to exit a queue at a stop line. Depending on the width of the cycling facility, bicyclists

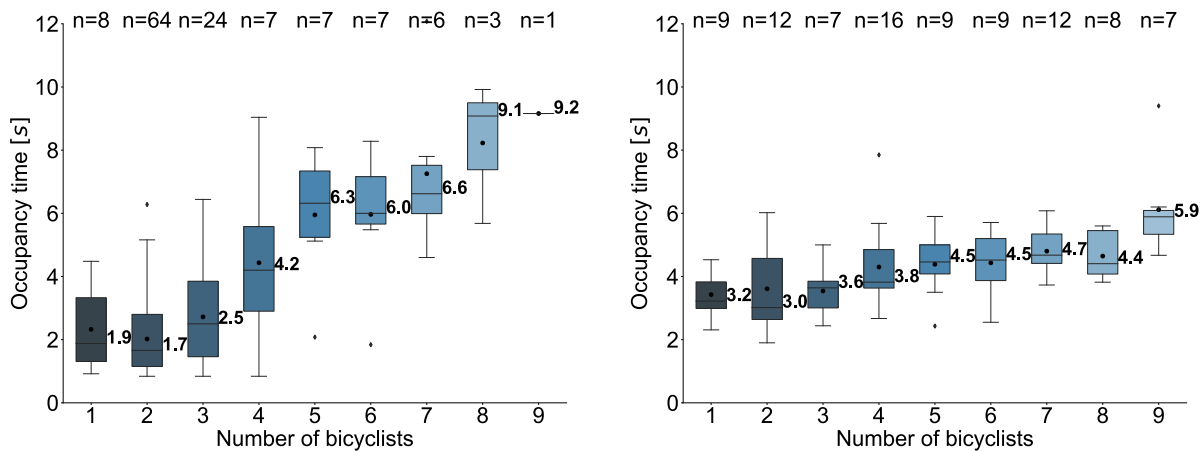
405 can ride two or more abreast, which makes it necessary to use a different method for
 406 determining the duration of queue discharge than used for motor vehicle traffic. Here, the
 407 duration of time between the beginning of the green phase and the moment the last bicyclist
 408 in the queue completely crosses the stop line is taken as the queue discharge time. This
 409 duration is divided by the number of bicyclists in the queue. Figure 8 (right) shows the
 410 average queue discharge values for different widths of the cycling facility. There is a slight
 411 upward trend in the average queue discharge time at a width of 2.5 m (in comparison to 2.0
 412 m). This likely stems from variation in the bicyclist behavior at the two approaches at the
 413 study intersection Kapuzinerplatz in Munich, or possibly indicate that bicycle lanes wider than
 414 2m may lead to bicyclists forming queue formations that do not discharge efficiently. In any
 415 case the data were collected at a single intersection with two approaches with that width size
 416 and therefore further research is required. The general trend, however, is that the average
 417 discharge time per bicyclist decreases as the width of the cycling facility increases. The
 418 sample size n refers to the number of analysed discharge processes.



419
 420 Figure 8 Observed queue density (left) and average discharge time (right) by infrastructure width.

- 421 • **Occupancy time:** This parameter is defined as the duration in seconds that the conflict area
 422 between right-turning motor vehicles and bicyclists riding straight across the intersection in
 423 the same direction is occupied by bicyclists. Only the group of bicyclists queued before the
 424 signal turned green is considered in the evaluation. The occupancy time is the duration that
 425 the conflict area is continuously occupied by at least one bicyclist. Bicyclists arriving during
 426 the green phase are not considered in the calculation of this parameter. Figure 9 (left) shows
 427 the occupancy times for bicyclist queues of different sizes on on-road and separated cycling
 428 facilities. The occupancy time on a bike box at the intersection Oranienburger Strasse /

429 Friedrichstrasse by the number of bicyclists in the queue size is shown in Figure 9 (right). The
 430 sample size n refers to the number of analysed bicyclist groups (group sizes $s = 1$ (individual
 431 bicyclist) to $s = 9$) occupying the conflict area at all relevant intersection approaches with a
 432 bicycle lane, a bicycle path or a bike box. The occupancy time is increasing stepwise together
 433 with the increase in the number of bicyclists, which might be explained by the fact that
 434 bicyclists can ride side by side across the conflict area. In the case of the bicycle box the
 435 occupancy time increases slightly with the increase in the number of bicyclists. This is
 436 attributed to the fact that the bike box has a sufficiently wide area that allows several
 437 bicyclists standing side by side to ride through the intersection approach at the start of green
 438 time.



439
 440 Figure 9 Observed occupancy times for on-road and separated cycling facilities (left) and bike boxes
 441 (right)

442 **4.2. Simulation Studies**

443 The developed simulation models are used to study the traffic performance parameters at typical
 444 intersection approaches with different types of bicycle infrastructure. Additionally, in the simulation
 445 studies increasing bicycle traffic volumes can be simulated that could not be observed in the
 446 empirical studies.

447 Therefore, it is important for the simulation models that the aggregation of the individual bicyclist
 448 dynamic and operational behaviour characteristics results in the accurate estimation of bicycle traffic
 449 flow performance indicators even for traffic flow compositions that either have not been or cannot be
 450 observed in the empirical studies. The empirical studies focused on the derivation of distributions of
 451 fundamental traffic parameters for individual bicyclists (speed, acceleration) and bicycle traffic flow
 452 (queue density, average discharge time) for different settings (e.g. lane width) rather than the

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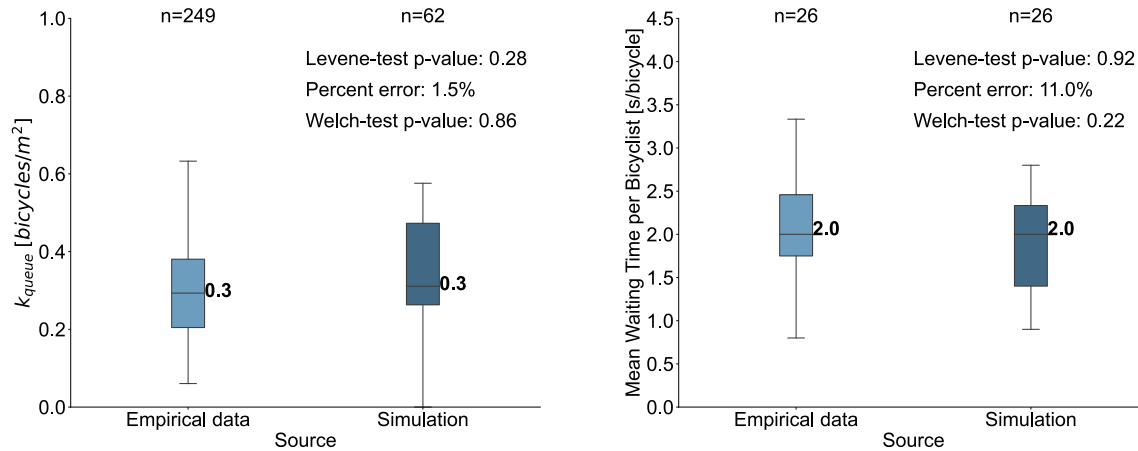
453 analysis of situations (e.g. days). This setting allows for model calibration but not for validation by out
454 of sample testing, since all usable observations make up the traffic parameter distributions and
455 random sampling from a distribution should lead to a similar distribution. Thus, in our research, we
456 distinguish between calibration (or adjustment) of input parameters and calibration based on
457 simulation output.

458 On the input side, acceleration functions and the desired speed distributions in PTV Vissim are set
459 according to the results of the empirical studies (Figure 7). Acceleration is crucial for the queue
460 discharge process with bicyclists starting from a complete stop to cross the stop line and eventually
461 clear the intersection. Desired speed might be a relevant factor for queue discharging and
462 intersection clearance as well (if the distance from the starting position to the stop line is long enough
463 to reach the desired speed).

464 On the output side, the empirically determined queue density, the average discharge time, and the
465 occupancy time are used to calibrate the parameters of the longitudinal and lateral behavior models.
466 Vehicular traffic is calibrated so that the discharge times and capacities for a given signal plan are
467 reproduced in accordance with HBS. Finally, the empirically observed effect of bicycle traffic on the
468 average discharge time of the first vehicle turning right is used to validate the simulation models.

469 Figure 10 shows comparisons of empirical data and simulation output for two traffic parameters.
470 Figure 10 (left) shows the queue density on bicycle lanes in front of a stop line in the simulation and
471 from the empirical studies. The simulated bicyclists form slightly denser queues than the observed
472 bicyclists, but the relative error of the means is small (percent error = 1.5 %). The median values,
473 rounded to one decimal place, are equal (0.3 bicycles/m²). The mean waiting times of motor vehicles
474 turning right per bicyclist crossing the intersection from the same approach is shown in Figure 10
475 (right). The relative error of the means is larger than for the density (percent error = 11 %), The
476 median values, rounded to one decimal place, are equal (2 s/bicycles).

477 Additionally, we further assess the simulation results through statistical testing. We use the Levene
478 test to evaluate the equality of variance between the two populations, as it is more robust in
479 comparison to the F-test which assumes distribution normality. The p-value is 0.28 (density) and 0.92
480 (waiting time), respectively, such that the null hypothesis of equal variances for both cases is
481 rejected. Therefore, the Welch-test is applied to determine if the hypothesis of equal means must be
482 rejected, as it performs better with unequal population sizes and variances. The null hypothesis of
483 equal means in both populations is rejected if the p-value is smaller than 0.05. The p-value is 0.86
484 (density) and 0.22 (waiting time), respectively, such that the null hypothesis of equal means for both
485 cases cannot be rejected, also indicating that simulation results are in accordance with the empirical
486 observations.



487

488 Figure 10 Comparison of the simulation results and the empirical findings: bicycle queue density at
 489 the stop line (left) and mean waiting time for right-turning vehicles per bicyclist crossing the
 490 intersection (right)

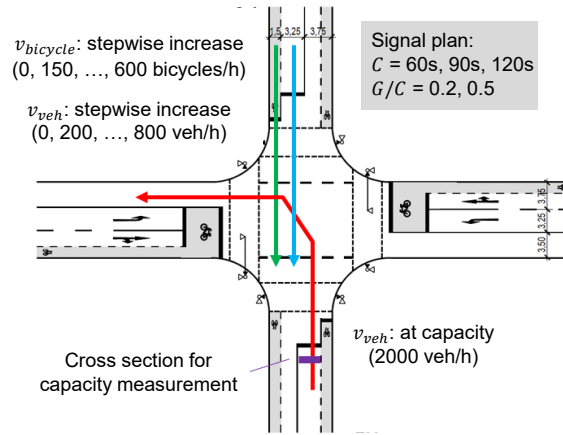
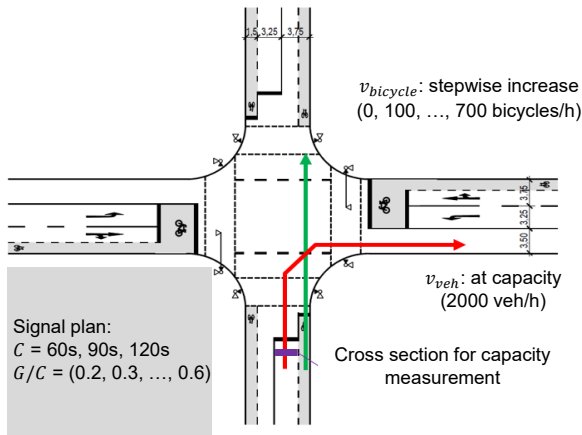
491 Only comparable cases from the empirical studies were used for the calibration of the simulation
 492 model. Therefore, all the simulation results depend on the relationships identified in the observed
 493 data and continue to apply beyond the range of observations. Respectively the direct applicability of
 494 results from such studies on real world applications may proceed with some caution, however the
 495 use of simulation tools is deemed as a necessary step towards the development of further
 496 methodologies when empirical data is insufficient, or their collection is not feasible.

497 A total of four simulation scenarios with typical infrastructure design and dimensions are examined.
 498 In the simulation scenarios, the bicycle volume $v_{bicycle}$, the vehicular volume v_{veh} , the signal cycle
 499 length C and the actual green time ratio (G/C) are systematically altered. Figure 11 presents the four
 500 scenarios and the parameter sets used. The capacity is analysed in all scenarios as this parameter is
 501 also used to determine the degree of capacity utilization, waiting time, congestion length, and Level
 502 of Service according to the HBS. The simulation results show the relationship between the bicycle
 503 volumes and capacities of the affected vehicular streams in each scenario.

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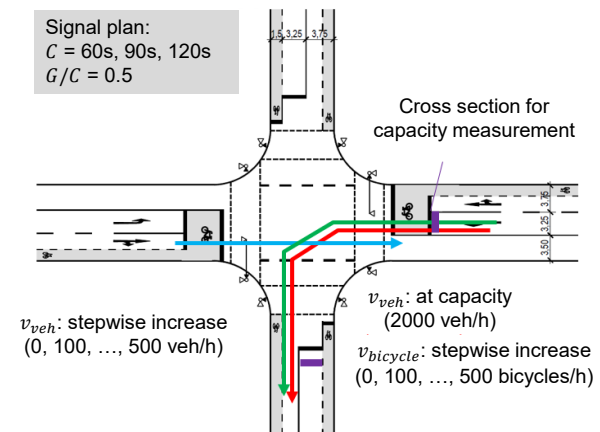
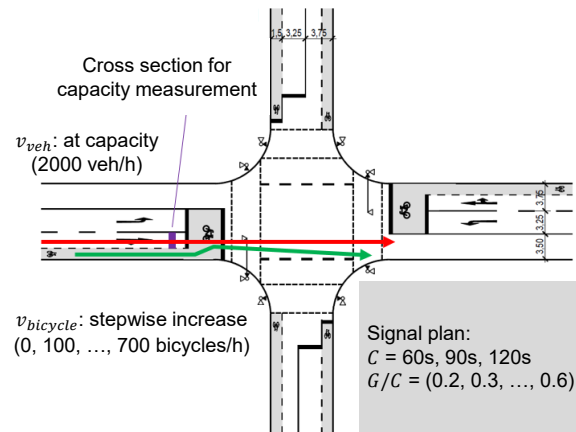
Scenario 1: Right-turning vehicles

Scenario 2: Left-turning vehicles



Scenario 3: Crossing vehicles (bike box)

Scenario 4: Left-turning vehicles (bike box)

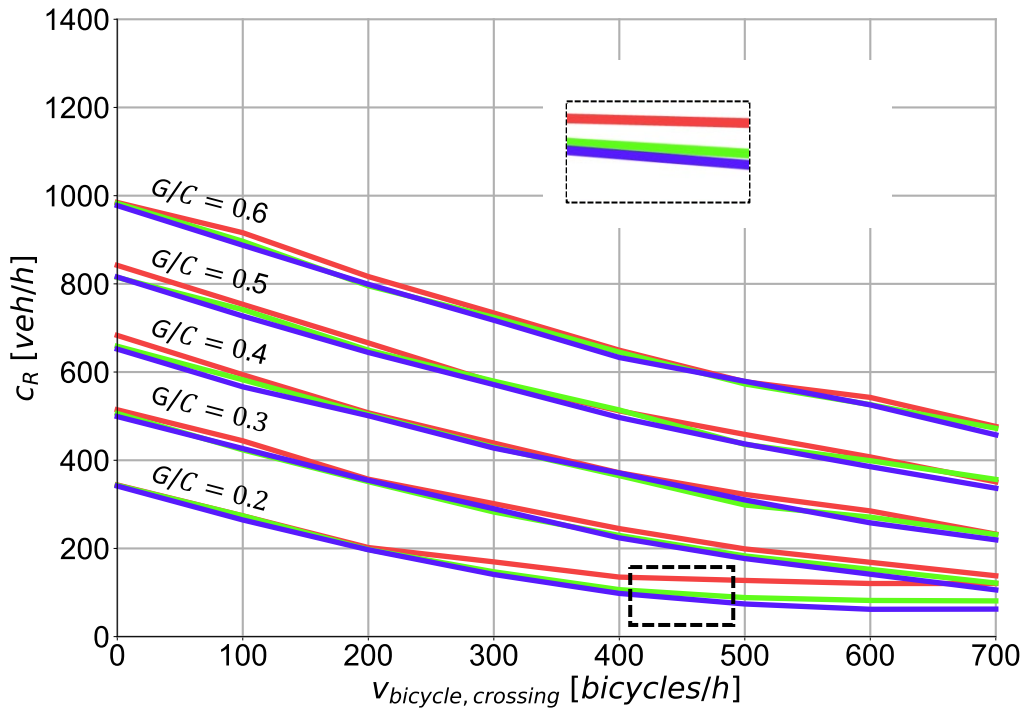


- Crossing motor vehicle traffic stream
- Bicycle traffic stream
- Motor vehicle traffic stream for capacity measurement

504 Figure 11 Overview of the simulation scenarios

505 **Scenario 1:** Capacity of right-turning vehicular traffic with parallel bicycle traffic crossing the
 506 intersection.

507 The capacity of the right-turning vehicular traffic decreases with the volume of bicycle traffic, as
 508 expected, but to a lesser extent at very high bicycle traffic volumes (see



509

510 Figure 12). Concerning signal control, the capacity is mainly influenced by the actual green time ratio

511 (G/C). However, it can also be observed that the cycle length C has an influence on the capacity at

512 very high bicycle traffic volumes and low actual green time ratios (G/C). The influence of the cycle

513 time depends on the distance between the stop line and the point of conflict between the right-turning

514 vehicles and the parallel crossing bicyclists, as vehicles waiting here can cross during the signal

515 phase change. The capacity of right-turning vehicles is dependent on the type of approach, as shown

516 in Figure 13. The average capacity of right-turning vehicles is slightly reduced in the case of a bike

517 box when compared to an intersection approach with a bike lane. Results also suggest that the

518 allocation of a bike path at the intersection approach improves the capacity of right turning vehicles in

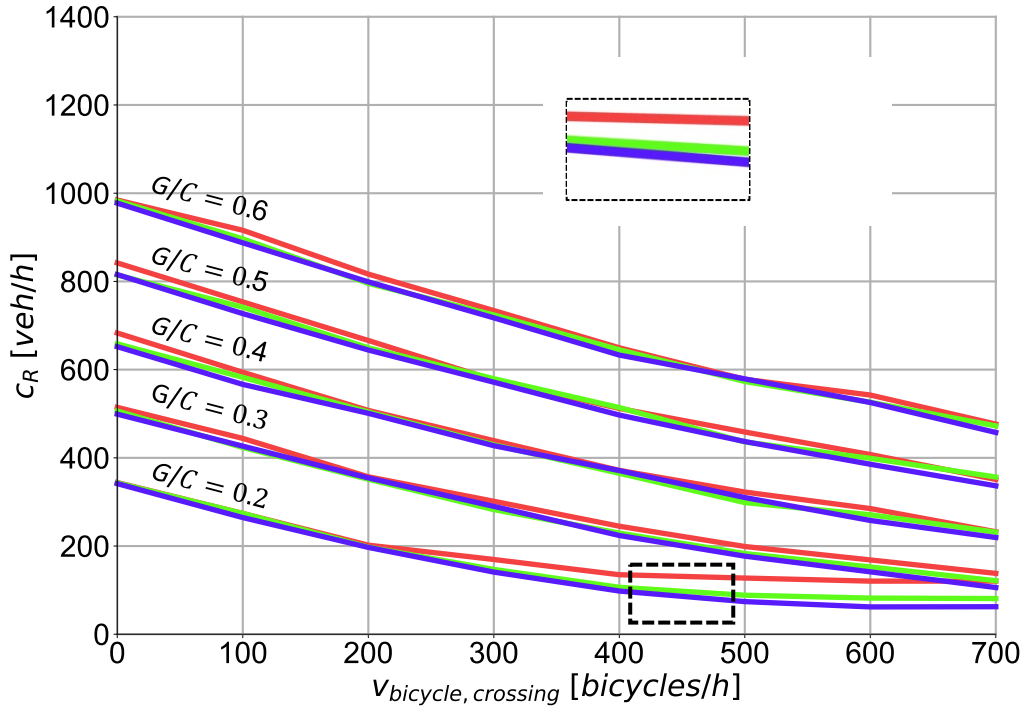
519 comparison to the other examined approach infrastructure. Therefore, in combination with the results

520 of the empirical analysis (see Figure 4) bike boxes are beneficial for facilitating direct left turns at the

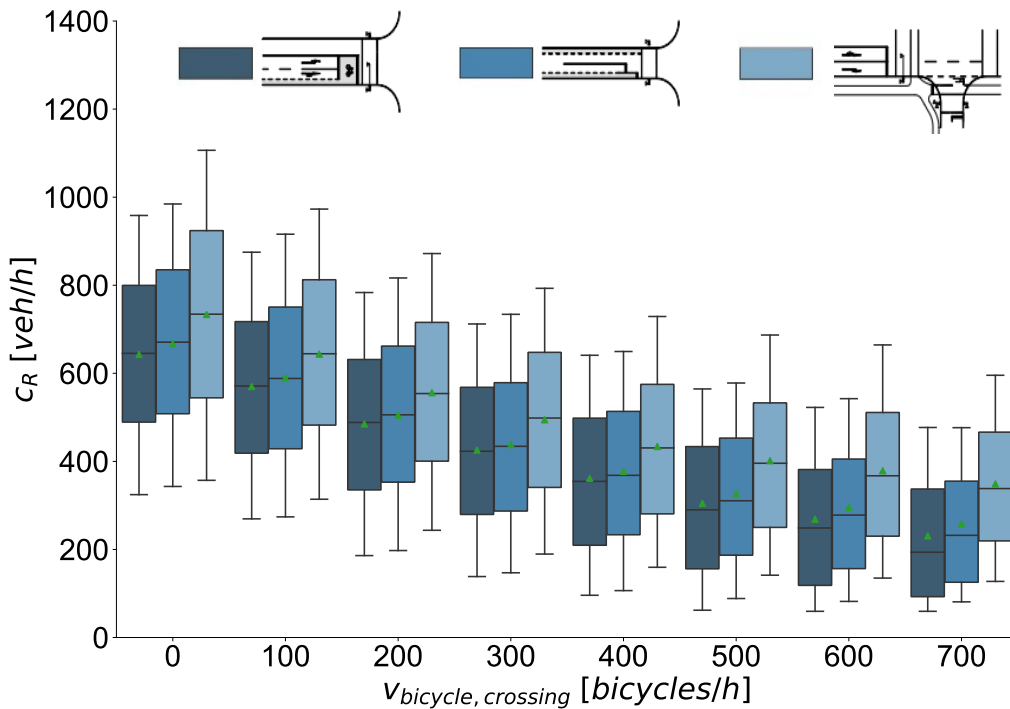
521 intersection approach for bicycle traffic, however in the absence of significant shares of left turning

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522 bicycle traffic as defined by the goals and policy of the respective transport authorities, the allocation
523 of a bicycle lane or a bicycle path offer improved capacity conditions for motor vehicle traffic.



524
525 Figure 12 Capacity of right-turning motor vehicles with parallel bicycle traffic riding straight at the
526 intersection approach.
527



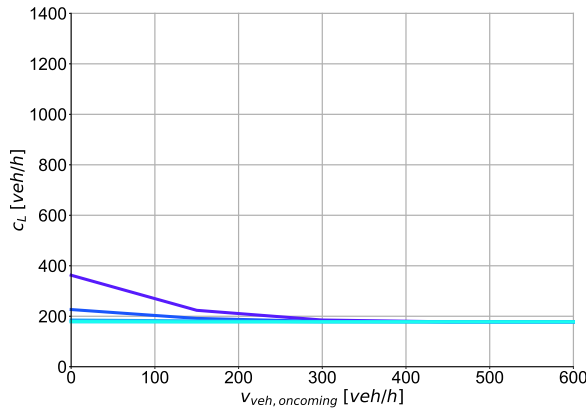
528

529 Figure 13 Capacity of right-turning vehicles by type of approach infrastructure ($C = 90 s$).

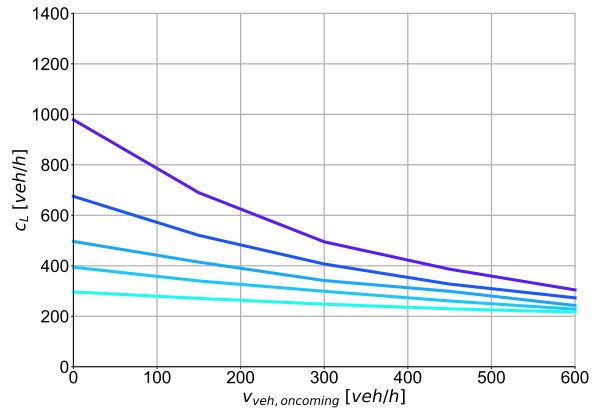
530 **Scenario 2:** Capacity of left-turning vehicular traffic with opposing bicycle and vehicular traffic
 531 crossing the intersection.

532 The capacity of left-turning vehicular traffic streams is strongly influenced by oncoming bicyclists and
 533 motor vehicles crossing the intersection. A comparison of the simulation studies (Figure 14) shows
 534 that the actual green time ratio (G/C) has a significant influence on the capacity of this vehicle
 535 stream. The effect of the cycle length C increases with the volume of oncoming motor vehicle and
 536 bicycle traffic. The higher the volume of oncoming motor traffic and the higher the volume of
 537 oncoming bicycle traffic, the more the capacity of the turning motor vehicle traffic stream is reduced,
 538 while a capacity threshold is reached at $c_L \approx 200veh/h$ ($C = 60s$) and $c_L \approx 100veh/h$ ($C = 120s$),
 539 where turning motor vehicles primarily turn off at the intersection during the integreen time. The
 540 longer the cycle length, the smaller the capacity becomes with the same actual green time ratio
 541 (G/C), which demonstrates the large influence of the capacity during phase changes.

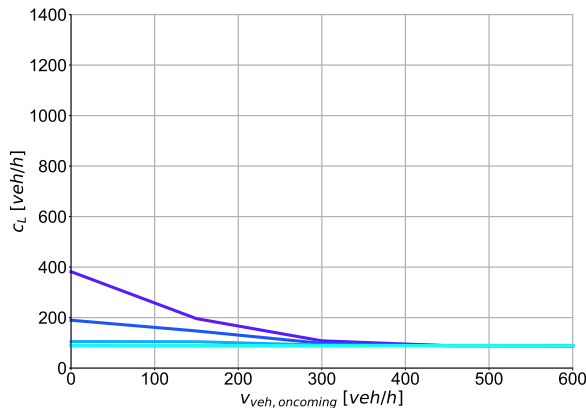
$C = 60s, G/C = 0.2$



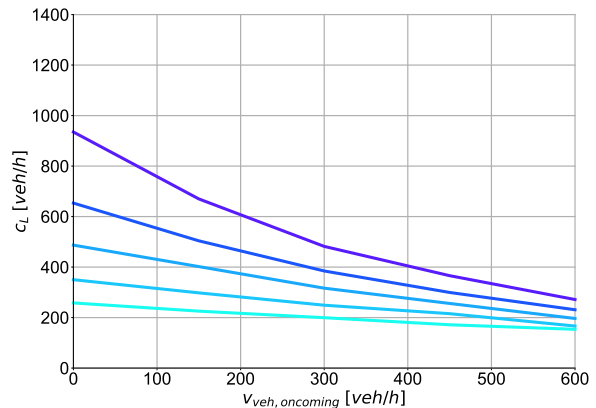
$C = 60s, G/C = 0.5$



$C = 120s, G/C = 0.2$



$C = 120s, G/C = 0.5$

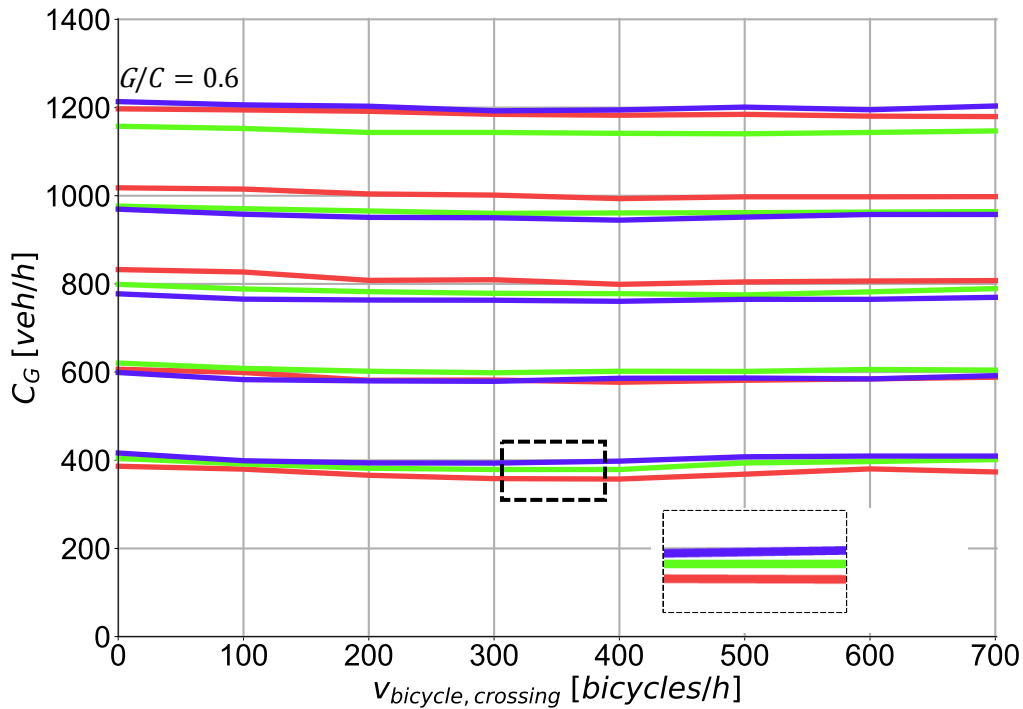


Bicycle traffic volume [bicycles/h] — $V_{bicycle, oncoming} = 200$ — $V_{bicycle, oncoming} = 600$
 — $V_{bicycle, oncoming} = 0$ — $V_{bicycle, oncoming} = 400$ — $V_{bicycle, oncoming} = 800$

542 Figure 14 Capacity of left-turning motor vehicle streams with opposing bicycle and motor vehicle
 543 traffic.

544 **Scenario 3:** Capacity of crossing vehicular traffic with parallel bicycle traffic crossing the intersection
 545 using a bike box.

546 Results (Figure 15) show that the vehicular capacity crossing the intersection is relatively
 547 independent of the volume of bicycle traffic crossing the intersection. Bicyclists crossing the
 548 intersection are observed to queue on the right side of the bike box and did not significantly affect the
 549 movement of motor vehicles crossing the intersection at the start of the green phase. This queuing
 550 behavior is carefully recreated in the simulations. With very large bicycle traffic volumes, the queue of
 551 bicyclists waiting on the right side of the bike box spills back into the bicycle lane such that bicyclists
 552 reaching the intersection cannot enter the bike box and do not influence the capacity of motor vehicle
 553 traffic.

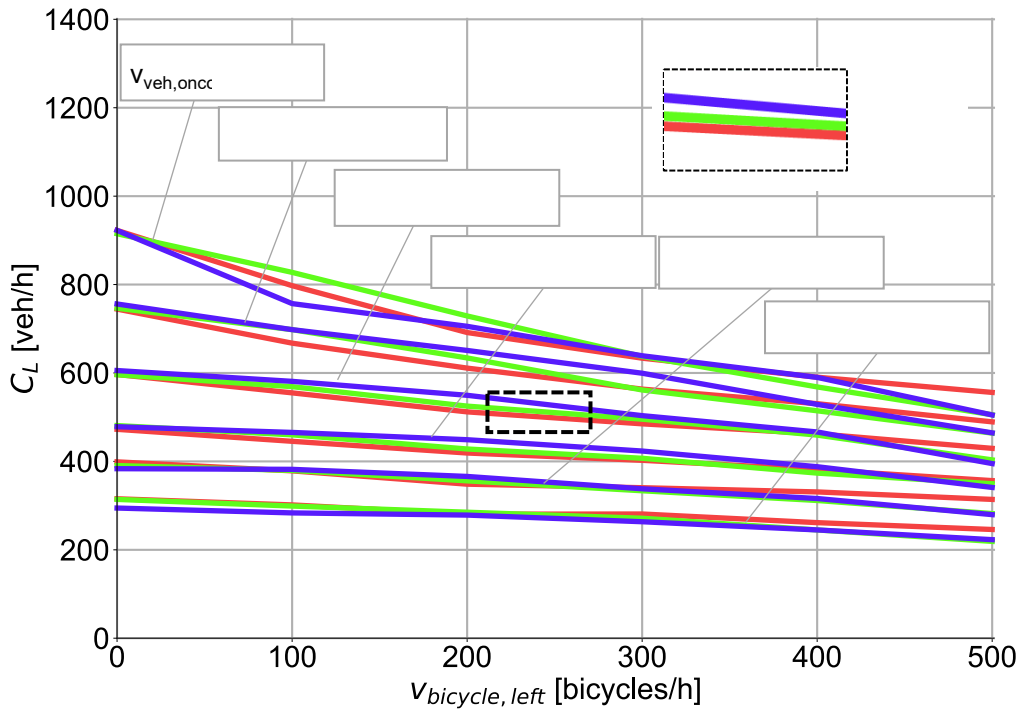


554

555 Figure 15 Capacity of crossing vehicular traffic with parallel bicycle traffic crossing the intersection
 556 using a bike box.

557 **Scenario 4:** Capacity of left-turning vehicular traffic with opposing bicycle traffic crossing the
 558 intersection with a bike box.

559 The vehicular capacity decreases as the number of cyclists turning left increases. When using a bike
 560 box, left-turning bicyclists queue in front of motor vehicles, and therefore the capacity of left-turning
 561 vehicle streams depends on the time gap acceptance of bicyclists turning left. With increasing
 562 volumes of oncoming bicyclists crossing the intersection, smaller time gaps can be expected, leading
 563 to a further reduction in capacity. Results are presented in Figure 16.



564

565 Figure 16 Capacity of left-turning vehicular traffic with opposing bicycle traffic crossing the
566 intersection with a bike box.

567 **5. Implications for Practice**

568 Several adjustments and extension to the design and evaluation approaches defined in the HBS are
569 proposed.

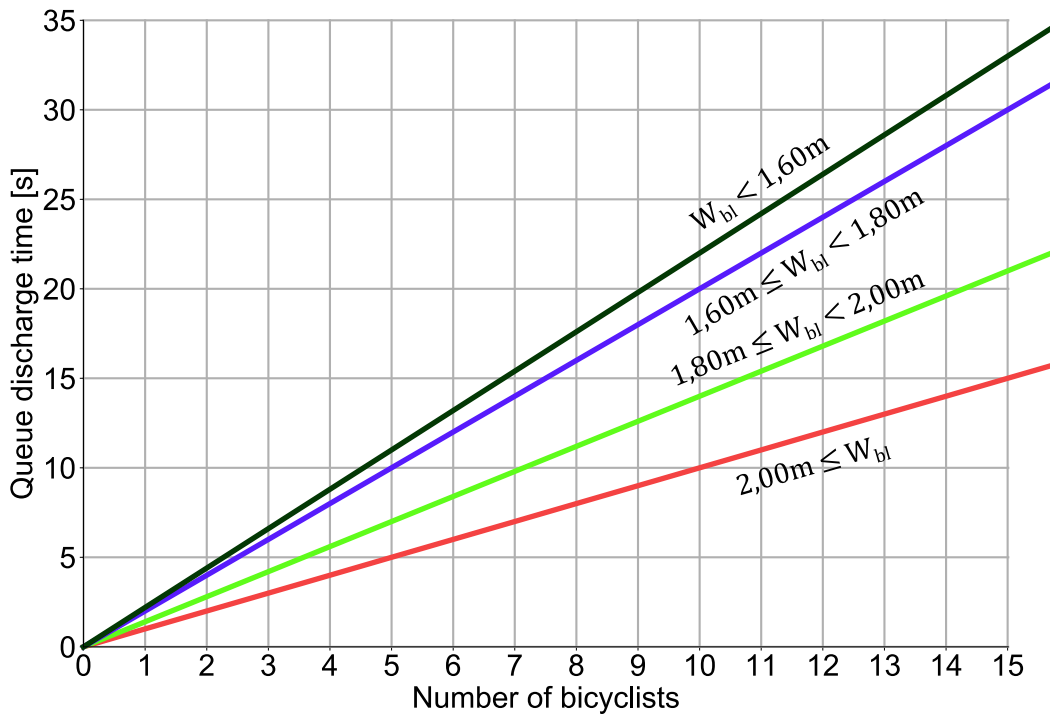
570 1. Discharge time for bicycle traffic on a separated cycling facility

571 The capacity of a cycling facility can be determined analogously to the capacity of vehicular traffic
572 with unobstructed flow using the discharge time per vehicle and the actual green time ratio (G/C).
573 This is of particular interest with large volumes of bicycle traffic because a queue can remain at the
574 end of a green phase. Based on the empirical data (see Figure 8), the observed bicycle density as a
575 function of the infrastructure width is only slightly decreasing, while the median bicycle queue density
576 is almost constant with increasing infrastructure width. Therefore, average queue discharge time $t_{W_{bl}}$
577 is defined as a function of the width of the cycling facility W_{bl} and is presented in Table 3. Figure 17
578 Queue discharge time for bicyclist groups by facility width.presents the expected queue discharge
579 times by facility width for bicyclist group sizes 1 to 15 using Table 3.

580

581 Table 3 Average discharge times for bicycle traffic by facility width.

W_{bl} [m]	$t_{W_{bl}}$ [s/bicycle]
≥ 2.00	1.0
$1.80 \leq W_{bl} < 2.00$	1.4
$1.60 \leq W_{bl} < 1.80$	2.0
< 1.60	2.2



582

583 Figure 17 Queue discharge time for bicyclist groups by facility width.

584 2. Influence of bicyclists in a bike box on crossing motor vehicle traffic

585 If a bike box is present, an effect on the capacity of vehicular traffic can only be detected if the
 586 volume of bicycle traffic is greater than approximately 100 bicycles/h (leading to more than one
 587 bicyclist arriving at red in the majority of the cases). Based on this finding, it is proposed to apply no
 588 time deduction for bicycle traffic volumes less than 100 bicycles/h and a time deduction of 1 s for
 589 bicycle traffic volumes greater than 100 bicycles/h.

590 3. Occupancy time of the conflict area between right-turning motor vehicles and parallel bicyclists
 591 crossing the intersection.

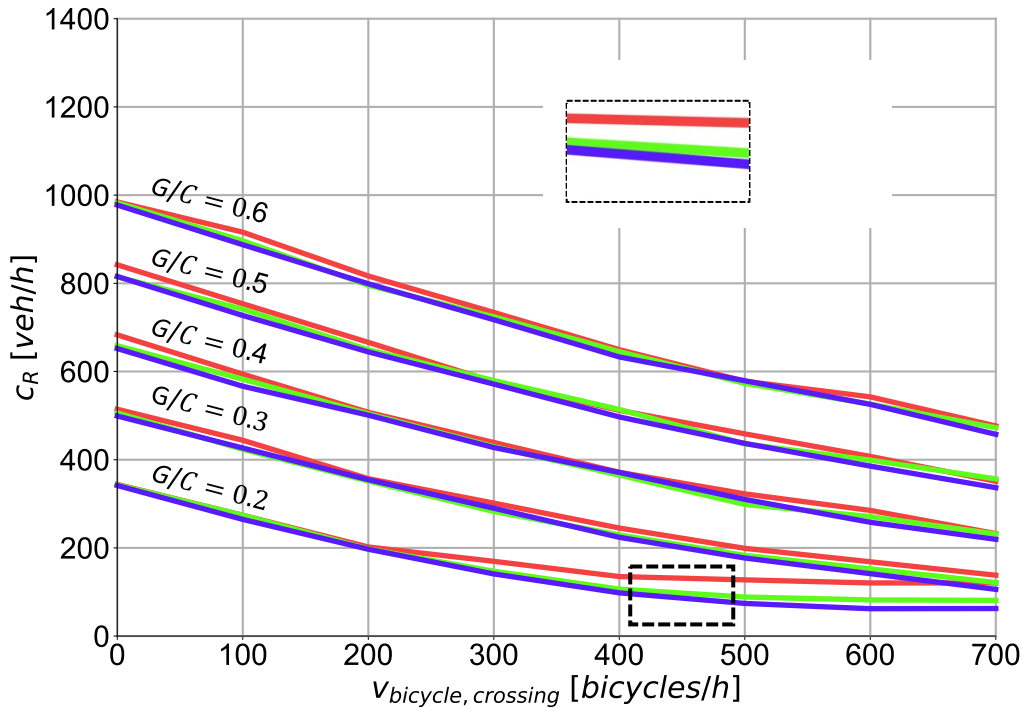
592 The empirical and simulation results show that the capacity of vehicular traffic depends on the
 593 volume of parallel bicycle traffic and the actual green time ratio (G/C) for motor vehicle traffic.

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594 Adjustment factors are typically used in both the HBS and HCM to account for the effect of different
 595 factors on unobstructed traffic flow at the respective traffic facility. Based on these findings, a factor
 596 for the reduction of the capacity of vehicular traffic with unobstructed outflow is derived:

$$c_{R,i} = c_{0,R,i} \cdot f_{cR,veh} \tag{1}$$

597 Where $c_{R,i}$ is the capacity of the right-turning motor vehicle stream i [veh/h], $c_{0,R,i}$ is the capacity of the
 598 right-turning motor vehicle stream i with unobstructed outflow using Equation S4-8 of the German HBS
 599 [veh/h] and $f_{cR,veh}$ is a factor to reduce the capacity of the right-turning traffic depending on the volume
 600 of parallel bicycle traffic and the actual green time ratio (G/C) for the motor vehicle traffic. The reduction
 601 factor is estimated from the results of the capacity of right-turning motor vehicle streams with parallel
 602 bicycle traffic (

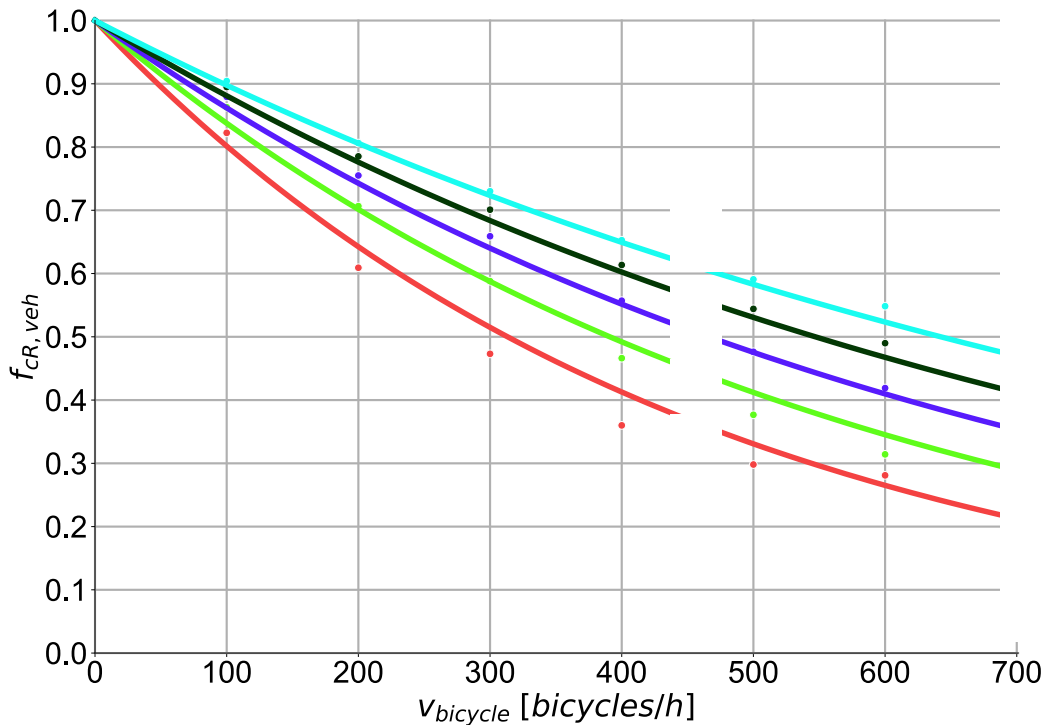


603
 604 Figure 12). Subsequently the capacity reduction share is estimated as a function of the capacity
 605 reduction divided by the free flow capacity ($v_{bicycle} = 0$). The reduction factor is formulated as a
 606 single function with decreasing G/C and increasing bicycle volumes $v_{bicycle}$ leading to stronger
 607 reduction of the capacity. The basic shape and the constants in the formula, as shown in Equation 2
 608 and Figure 18, are found by regression.

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$$f_{cR,veh} = e^{-\left(\frac{1}{\sqrt{G/C \cdot 1000}} - \frac{(G/C)^2}{sR \cdot 0,85}\right) v_{bicycle}} \quad (2)$$

609 Where C is the cycle length, (G/C) is the actual green time ratio for the right-turning vehicular traffic,
 610 s_{veh} is the saturation flow of right-turning vehicular traffic [veh/h] and $v_{bicycle}$ is the flow of parallel
 611 bicycle traffic [bicycles/h].
 612



613
 614 Figure 18 Factor for reducing the capacity of right-turning vehicular traffic based on bicycle traffic flow
 615 and actual green time ratio (G/C).

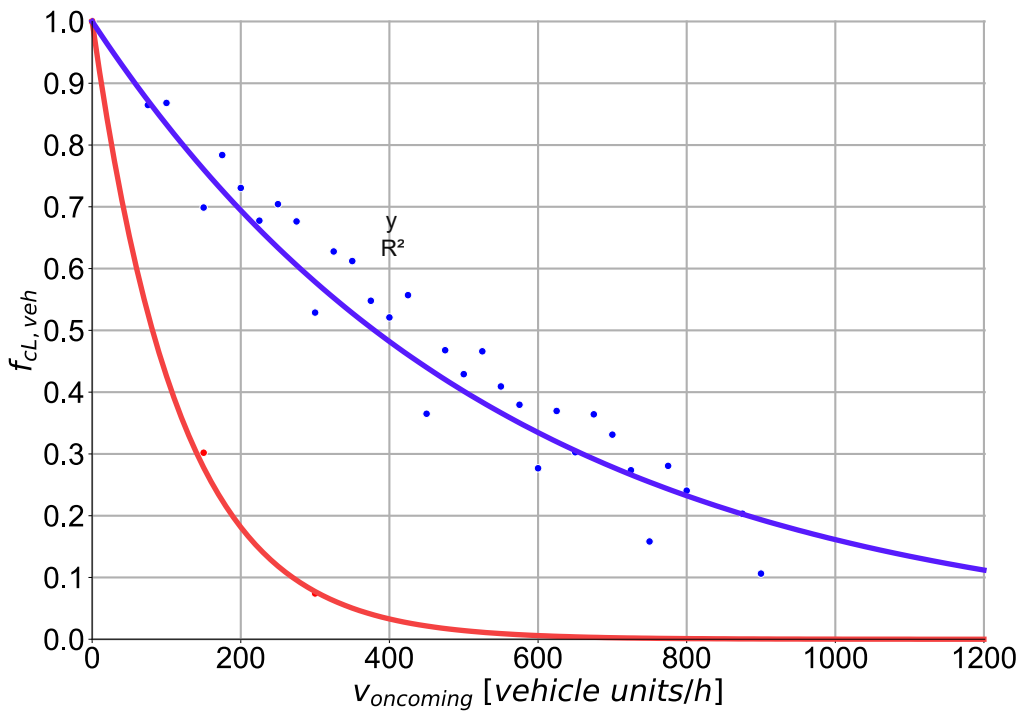
616 4. Influence of oncoming bicycle traffic on left-turning motor vehicle traffic

617 As expected, and as the simulation results show, oncoming motor vehicle and bicycle traffic have a
 618 considerable influence on the capacity of the left-turning vehicular traffic flows. Indeed, the capacity
 619 reduction for left-turning vehicle traffic due to oncoming motor vehicles and bicyclists is directly
 620 dependent on these two volumes. For this purpose, a conversion to vehicle units with 0.75 cyclists =
 621 1 vehicle unit is suggested. $c_{L,i}$ is the capacity of the left-turning motor vehicle stream i and is
 622 derived using Equation 3.

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$$c_{Lc,i} = c_{0,L,i} \cdot f_{cL,veh} \tag{3}$$

623 Where $c_{0,L,i}$ is the capacity of the left-turning motor vehicle stream i with unobstructed outflow
 624 using Equation S4-8 of the HBS. $f_{cL,veh}$ is the reduction factor for the capacity for left-turning
 625 vehicular traffic depending on the green time (G/C) ratio for the left-turning motor vehicle traffic, as
 626 shown in Figure 19. The reduction factor is estimated from the results of the capacity of left-turning
 627 motor vehicle streams with opposing bicycle and motor vehicle traffic (Figure 14), where the bicycle
 628 and motor vehicle traffic volumes are aggregated into vehicle units. Subsequently the capacity
 629 reduction share is estimated as a function of the capacity reduction divided by the free flow capacity
 630 ($v_{oncoming} = 0$). A regression function is then used to model the capacity reduction and derive the
 631 reduction factor for the respective green time (G/C) ratios.



632
 633 Figure 19 Factor for reducing the capacity of left-turning traffic based on the combined bicycle and
 634 vehicular traffic flow and actual green time ratio.

635 **6. Conclusion**

636 The aim of this research is to investigate traffic flow at signalized intersections with large volumes of
 637 bicycle traffic and based on this, to review the existing calculation method in the HBS as well as other
 638 official design manuals, such as the HCM, for determining traffic quality and, if necessary, adapt or

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639 extend the present methods. Empirical data were collected and used to build, calibrate, and validate
640 microscopic traffic simulation models. Data are generated with the resulting simulation models for
641 situations with large bicycle traffic volumes as the empirical investigations could not cover all
642 situations and the entire spectrum of relevant vehicle and bicycle traffic volumes.

643 Microscopic traffic simulation proved to be a suitable instrument for generating data for the
644 verification and further development of the calculation methods. The behavior of cyclists and motor
645 vehicles in traffic are parametrized to create realistic bicycle and vehicular traffic flows. Additionally,
646 the data required for the development of calculation methods can be generated and output relatively
647 directly using microscopic traffic simulation tools. While extensive findings are now available on the
648 speeds, accelerations, and queuing and queue dispersion behavior of cyclists, detailed information
649 concerning the acceptance of time gaps for the parameterization of the models is still lacking. While
650 the results from the model extrapolate the results of the empirical studies, still results for higher or
651 saturated traffic flows have not been verified with empirical data. Finally, our developed methods are
652 based on empirical data collected only at intersections in Germany with specific types of bicycle
653 infrastructure and traffic conditions. The behavior of bicyclists across all study intersections did not
654 seem to vary significantly however it is expected that the driving behavior of bicyclists in other
655 countries or in different traffic situations might deviate from our observations.

656 Based on the empirical and simulation results, additions and/or adaptations to the calculation method
657 in HBS are suggested for the following aspects:

- 658 • Management of bicycle traffic on a dedicated cycling facility (bicycle path or bicycle lane),
- 659 • Consideration of the influence of bicyclist queue formation and discharge with a bike box,
- 660 • Consideration of the influence of parallel crossing bicycle traffic on the capacity of right-
661 turning motor vehicle traffic,
- 662 • Consideration of the influence of bicyclists in oncoming traffic on the capacity of the left-
663 turning motor vehicle traffic.

664 The proposed adjustments and extensions to the design and evaluation approaches for the German
665 HBS can be integrated or used together with the HCM in the process of calculating the adjustment
666 factor values for vehicular capacity. The findings for the bike boxes and the proposed time deduction
667 can be integrated into the HCM in cases, where such bicycle infrastructure is provided. Also, the
668 proposed adjustment factors $f_{cR,veh}$ and $f_{cL,veh}$ for the capacity of right and left turning vehicular
669 traffic can be used to account for the influence of the bicycle flow independently of that of the
670 pedestrian flow or for cases with minimal to no pedestrian interference.

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671 Future research to extend the results presented in this paper could focus on the collection and
672 analysis of empirical data during events of bicyclist congestion, the extension of the calculation
673 methods for bicyclists in mixed traffic (with and without protective strips) and the resulting passing on
674 the right of a queue of motor vehicles, the effect of pedestrians on bicyclists turning right and left at
675 an intersection and the consideration of indirect left-turning bicyclists.

676 **7. Acknowledgments**

677 This research is conducted for the Project FE 70.0925/2015 “Verkehrsablauf an signalisierten
678 Knotenpunkten mit hohem Radverkehrsaufkommen” (Traffic Flow at Signalized Intersections with
679 High Bicycle Traffic Volumes) funded by the “Bundesanstalt für Straßenwesen (BASt)” (Federal
680 Highway Research Institute of Germany).

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681 8. References

- 682 Allen, D., Bygrave, S., Harper, H., 2005. Behaviour at cycle advanced stop lines. Transport for London
683 (TRL).
- 684 Allen, D., Hummer, J., Roupail, N., Milazzo, J., 1998. Effect of bicycles on capacity of signalized
685 intersections. Transp. Res. Rec. J. Transp. Res. Board 1646 , 87–95.
- 686 Alrutz, D., Bohle, W., Müller, H., Prahlow, H., Hacke, U., Lohmann, G., 2009. Unfallrisiko und
687 Regelakzeptanz von Fahrradfahrern. Berichte der Bundesanstalt für Straßenwesen, Unterr.
688 Verkehrstechnik 184, 1–127.
- 689 Angenendt, W., Blase, A., Klöckner, D., 2005. Verbesserung der Radverkehrsführung an Knoten.
- 690 Baumann, F., 2016. Berner Ampeln stehen auf grün [WWW Document]. Velojournal. URL
691 <http://www.velojournal.ch/vj-online/nachrichten/2016/berner-ampeln-stehen-auf-gruen.html> (accessed
692 4.4.17).
- 693 Botma, H., Papendrecht, H., 1991. Traffic Operation Of Bicycle Traffic. Transp. Res. 1320 , 65–72.
- 694 Busch, F., Grigoropoulos, G., Kathis, H., Baier, M., Reinartz, A., Schuckließ, L., Junghans, M., Lücken, L.,
695 Leonhardt, A., 2019. Verkehrsablauf an signalisierten Knotenpunkten mit hohem
696 Radverkehrsaufkommen – Schlussbericht FE 70.0925/2015.
- 697 Chen, J., Wang, W., Li, Z., Jiang, H., Chen, X., Zhu, S., 2014. Dispersion Effect in Left-turn Mixed Bicycle
698 Traffic and Its Influence on Capacity of Left-turn Vehicles at Signalized Intersections, in:
699 Transportation Research Board, 93rd Annual Meeting. doi:10.3141/2468-05
- 700 Chen, X., Shao, C., Li, D., Dong, C., 2009. Capacity reliability of signalized intersections with mixed traffic
701 conditions. Tsinghua Sci. Technol. 14 3 , 333–340.
- 702 COWI, 2013. Micro Simulation of Cyclists in Peak Hour Traffic.
- 703 Deutsches Zentrum für Luft and Raumfahrt, 2020. UTRaCar and MoMoCar [WWW Document]. URL
704 https://www.dlr.de/ts/desktopdefault.aspx/tabid-1237/5441_read-12153%0A (accessed 9.17.20).
- 705 Falkenberg, G., Blase, A., Bonfranchi, T., Cosse, L., Draeger, W., Vortisch, P., Kautzsch, L., Stapf, H.,
706 Zimmermann, A., 2003. Bemessung von Radverkehrsanlagen unter verkehrstechnischen
707 Gesichtspunkten. Berichte Der Bundesanstalt Fuer Strassenwesen. Unterr. Verkehrstechnik 103 .
- 708 Figliozzi, M., Wheeler, N., Monsere, C., 2013. A Methodology to Estimate Bicyclists' Acceleration and
709 Speed Distributions at Signalized Intersections. Transp. Res. Rec. J. Transp. Res. Board 2387, 66–
710 75.
- 711 Forschungsgesellschaft für Straßen- und Verkehrswesen (FGSV), 2015. Handbuch für die Bemessung
712 von Straßenverkehrsanlagen (HBS).

PREPRINT

Please cite: 1.Grigoropoulos, Georgios; Leonhardt, A.; Kath, H.; Junghans, M.; Baier, M.; & Busch, F. (2022). Traffic flow at signalized intersections with large volumes of bicycle traffic. Transportation Research Part A: Policy and Practice. <https://doi.org/10.1016/j.tra.2021.11.021>

- 713 Forschungsgesellschaft für Straßen und Verkehrswesen (FGSV), 2010. Empfehlungen für
714 Radverkehrsanlagen (ERA), 2010th ed. Forschungsgesellschaft für Straßen- und Verkehrswesen
715 (Hrsg.), Köln.
- 716 Forschungsgesellschaft für Straßen und Verkehrswesen (FGSV), 2006. Richtlinien für die Anlage von
717 Stadtstraßen (RASt). Köln.
- 718 Greibe, P., Buch, T.S., 2016. Capacity and Behaviour on One-way Cycle Tracks of Different Widths.
719 Transp. Res. Procedia 15, 122–136. doi:10.1016/j.trpro.2016.06.011
- 720 Grigoropoulos, G., Kazakovtsev, S.M.M., Kath, H., Krämer, K., 2019. Evaluation of a Traffic Signal
721 Coordination for Bicycles in a Mixed Motor Vehicle and Public Transport Urban Network. Cycl. Res.
722 Board 2019.
- 723 Grigoropoulos, G., Twaddle, H., Spangler, M., Hagenbring, M., Düsterwald, M., 2018. Evaluierung der
724 dynamischen Grünen Welle für Radfahrer-Sittraffic SiBike-in Marburg. Straßenverkehrstechnik 268–
725 274.
- 726 Guo, Y., Yu, Q., Zhang, Y., Rong, J., 2012. Effect of Bicycles on the Saturation Flow Rate of Turning
727 Vehicles at Signalized Intersections. J. Transp. Eng. 138 1 , 21–30. doi:10.1061/(ASCE)TE.1943-
728 5436.0000317
- 729 Hein, M., Conference, G., Hutchison, D., 2013. LNCS 8142 - Pattern Recognition.
- 730 Hoegh, N., 2007. Green waves for cyclists in Copenhagen Denmark - Copenhagen. Work. Velo-city “From
731 Vis. to reality.”
- 732 Jin, S., Shen, L., Liu, M., Ma, D., 2017. Modelling speed–flow relationships for bicycle traffic flow. Proc.
733 Inst. Civ. Eng. Transp. 170 4 , 194–204. doi:10.1680/jtran.15.00115
- 734 Karl, M., Felix, B., 2013. Koordinierung von Lichtsignalanlagen fuer den Radverkehr.
735 Straßenverkehrstechnik.
- 736 Kath, H., Grigoropoulos, G., Krämer, K., 2019. Green signal countdown timers for bicycle traffic–Results
737 from a field study. Cycl. Res. Board 2019.
- 738 Kuller, E.C., Gersemann, D., Ruwenstroth, G., 1986. Regelabweichendes Verhalten von Fahrradfahrern.
739 Forschungsberichte Der Bundesanstalt Für Straßenwesen, Bereich Unfallforsch. 142 .
- 740 Kwigizile, V., Oh, J., Ikonov, P., Hasan, R., Villalobos, C.G., Kurdi, A.H., Shaw, A., 2017. Real Time
741 Bicycle Simulation Study of Bicyclists ' Behaviors and their Implication on Safety FINAL REPORT.
- 742 Landeshauptstadt München, 2019. Daten zum Radverkehr [WWW Document].
- 743 Landis, B.W., Vattikuti, V.R., Ottenberg, R.M., Petritsch, T.A., Guttenplan, M., Crider, L.B., 2003.
744 Intersection level of service for the bicycle through movement. Pedestrians Bicycl. 2003 Saf. Hum.

PREPRINT

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- 745 Perform. 1828 1828 , 101–106. doi:10.3141/1828-12
- 746 Li, Zhibin, Li, Zheng, Huang, R., Yang, Z., Zhou, W., Ye, M., 2015. Operational Features in Bicycle Traffic
747 Flow : An Observational Study 328.
- 748 Michon, J.A., 1985. A critical view of driver behavior models: what do we know, what should we do? *Hum.*
749 *Behav. traffic Saf.* 485–520. doi:10.1007/978-1-4613-2173-6
- 750 National Association of City Transportation Officials (NACTO), 2014. *Urban Bikeway Design Guide*. Island
751 Press.
- 752 National Research Council, 2016. *Highway Capacity Manual*, Transportation Research Board.
753 Transportation Research Board, Washington DC.
- 754 Nobis, C., Kuhnimhof, T., 2019. *Mobilität in Deutschland – MiD Analysen zum Radverkehr und*
755 *Fußverkehr*.
- 756 Opiela, K.S., Khasnabis, S., Datta, T.K., 1980. Determination of the characteristics of bicycle traffic at
757 urban intersections. *Transp. Res. Rec.* 743, 30–38.
- 758 Parkin, J., Rotheram, J., 2010. Design speeds and acceleration characteristics of bicycle traffic for use in
759 planning, design and appraisal. *Transp. Policy* 17 5 , 335–341. doi:10.1016/j.tranpol.2010.03.001
- 760 Peter Koonce, 2015. *Bicycle Countdown Signal - Time to Green* [WWW Document]. URL
761 <http://koonceportland.blogspot.de/2011/07/bicycle-countdown-signal-time-to-green.html> (accessed
762 11.27.15).
- 763 Petzoldt, T., Schleinitz, K., Krems, J.F., Gehlert, T., 2017. Drivers' gap acceptance in front of approaching
764 bicycles—Effects of bicycle speed and bicycle type. *Saf. Sci.* 92, 283–289.
- 765 Preethi, P., Varghese, A., Ashalatha, R., 2016. Modelling Delay at Signalized Intersections under
766 Heterogeneous Traffic Conditions. *Transp. Res. Procedia* 17 December 2014 , 529–538.
767 doi:10.1016/j.trpro.2016.11.107
- 768 Pu, Z., Li, Z., Wang, Y., Ye, M., Fan, W., 2017. Evaluating the Interference of Bicycle Traffic on Vehicle
769 Operation on Urban Streets with Bike Lanes. *J. Adv. Transp.* 2017. doi:10.1155/2017/6973089
- 770 Schleinitz, K., Petzoldt, T., Franke-Bartholdt, L., Krems, J., Gehlert, T., 2016. The German Naturalistic
771 Cycling Study – Comparing cycling speed of riders of different e-bikes and conventional bicycles.
772 *Saf. Sci.* doi:http://dx.doi.org/10.1016/j.ssci.2015.07.027
- 773 Taylor, D.B., 1993. Analysis of Traffic Signal Clearance Interval Requirements for Bicycle-Automobile
774 Mixed Traffic. *Transp. Res. Rec. J. Transp. Res. Board* 1405, 13–20.
- 775 Twaddle, H., 2017. Development of tactical and operational behaviour models for bicyclists based on
776 automated video data analysis. Technische Universität München.

PREPRINT

Please cite: 1.Grigoropoulos, Georgios; Leonhardt, A.; Kathis, H.; Junghans, M.; Baier, M.; & Busch, F. (2022). Traffic flow at signalized intersections with large volumes of bicycle traffic. Transportation Research Part A: Policy and Practice. <https://doi.org/10.1016/j.tra.2021.11.021>

- 777 Twaddle, H., Busch, F., 2019. Binomial and multinomial regression models for predicting the tactical
778 choices of bicyclists at signalised intersections. *Transp. Res. Part F Traffic Psychol. Behav.* 60, 47–
779 57. doi:10.1016/j.trf.2018.10.002
- 780 Twaddle, H., Grigoropoulos, G., 2016. Modeling the speed, acceleration and deceleration of bicyclists for
781 microscopic traffic simulation. *Transp. Res. Rec. (TRR), J. Transp. Res. Board.*
- 782 Wierbos, M.J., Knoop, V.L., Goñi-Ros, B., Hoogendoorn, S.P., 2020. The Influence of Jam Density and
783 Merging Cyclists on the Queue Discharge Rate. *J. Adv. Transp.* 2020. doi:10.1155/2020/9272845
- 784 Wierbos, M.J., Knoop, V.L., Hänseler, F.S., Hoogendoorn, S.P., 2019. Capacity, Capacity Drop, and
785 Relation of Capacity to the Path Width in Bicycle Traffic. *Transp. Res. Rec.* 2673 5 , 693–702.
786 doi:10.1177/0361198119840347
- 787